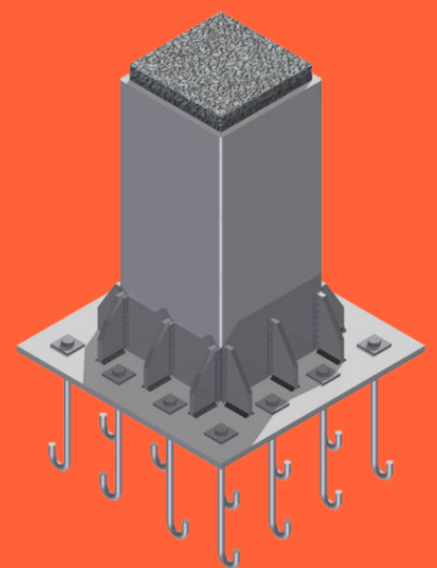
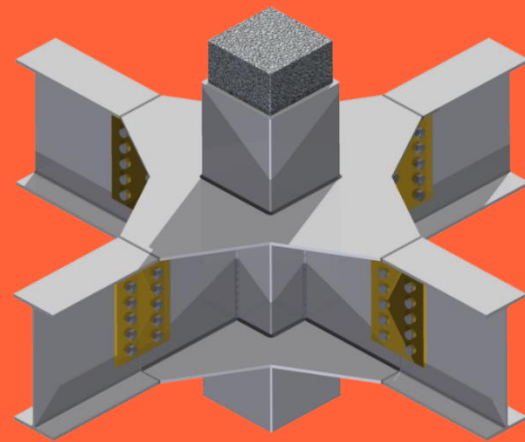


EXAMPLE CALCULATIONS – to the Requirements of BC4: 2015





Example Calculations to the Requirements of BC4: 2015

NOTE

1. Whilst every effort has been made to ensure accuracy of the information contained in this design guide, the Building and Construction Authority (“BCA”) makes no representations or warranty as to the completeness or accuracy thereof. Information in this design guide is supplied on the condition that the user of this publication will make their own determination as to the suitability for his or her purpose(s) prior to its use. The user of this publication must review and modify as necessary the information prior to using or incorporating the information into any project or endeavour. Any risk associated with using or relying on the information contained in the design guide shall be borne by the user. The information in the design guide is provided on an “as is” basis without any warranty of any kind whatsoever or accompanying services or support.
2. Nothing contained in this design guide is to be construed as a recommendation or requirement to use any policy, material, product, process, system or application and BCA makes no representation or warranty express or implied. NO REPRESENTATION OR WARRANTY, EITHER EXPRESSED OR IMPLIED OF FITNESS FOR A PARTICULAR PURPOSE IS MADE HEREUNDER WITH RESPECT TO INCLUDING BUT NOT LIMITED, WARRANTIES AS TO ACCURACY, TIMELINES, COMPLETENESS, MERCHANTABILITY OR FITNESS FOR A PARTICULAR PURPOSE OR COMPLIANCE WITH A PARTICULAR DESCRIPTION OR ANY IMPLIED WARRANTY ARISING FROM THE COURSE OF PERFORMANCE, COURSE OF DEALING, USAGE OF TRADE OR OTHERWISE, TO THE FULLEST EXTENT PERMITTED BY LAW. In particular, BCA makes no warranty that the information contained in the design guide will meet the user’s requirements or is error-free or that all errors in the drawings can be corrected or that the drawings will be in a form or format required by the user.
3. In no event will BCA be responsible or liable for damages of any kind resulting from the use or reliance upon information or the policies, materials, products, systems or applications to which the information refers. In addition to and notwithstanding the foregoing, in no event shall BCA be liable for any consequential or special damages or for any loss of profits incurred by the user or any third party in connection with or arising out of use or reliance of this design guide.

Copyright @ 2015 Building and Construction Authority, Singapore.

All rights reserved. This document or any part thereof may not be reproduced for any reason whatsoever in any form or means whatsoever and howsoever without the prior written consent and approval of the Building and Construction Authority.

Whilst every effort has been made to ensure the accuracy of the information contained in this publication, the Building and Construction Authority, its employees or agents shall not be responsible for any mistake or inaccuracy that may be contained herein and all such liability and responsibility are expressly disclaimed by these said parties.

Table of Contents

Introduction	v
1 Example 1.....	1
1.1 General	1
1.2 CHS 508x12.5 - S355 steel tube infilled with C40/50 concrete	1
1.3 CHS 508x12.5 - S355 steel tube infilled with C90/105 concrete	5
1.4 CHS 508x12.5 - S460 steel tube infilled with C40/50 concrete	7
1.5 CHS 406x12 - S460 steel tube infilled C90/105 concrete	8
1.6 Summary	11
2 Example 2.....	12
2.1 General	12
2.2 CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C50/60 concrete and G460 reinforcements	13
2.3 CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C90/105 concrete and G460 reinforcements	22
2.4 CHS 508x12.5 and UC 254x254x107 - S500 steel sections with C50/60 concrete and G460 reinforcements	25
2.5 Comparison and summary	27
3 Example 3.....	29
3.1 General	29
3.2 RHS 400x600x20 - S355 steel tube infilled with C50/60 concrete	30
3.3 RHS 400x600x20 - S355 steel tube infilled with C90/105 concrete	39
3.4 RHS 400x600x20 - S500 steel tube infilled with C50/60 concrete	41
3.5 RHS 400x600x20 - S500 steel tube infilled with C90/105 concrete	42
3.6 Comparison and summary	44

Introduction

This guidebook provides 3 worked examples to describe a step-by-step procedure for determining the design resistance of Concrete Filled Steel Tubular (CFST) columns in accordance with the requirements of BC4: 2015 - Design Guide for Concrete Filled Tubular Members with High Strength Materials to Eurocode 4.

In Example 1, the axial buckling resistance of a circular CFST column subject to pure compression is determined; In Example 2, a circular CFST column with encased UC section and reinforcements is checked against combined compression and uniaxial bending moment; In Example 3, a rectangular CFST column is designed for combined compression and bi-axial bending moments. For each Example, the steel and concrete strengths vary and the benefit by using high strength concrete (HSC) and high tensile steel (HTS) are evaluated.



1 Example 1

1.1 General

In Example 1, the axial buckling resistance of a concrete filled steel tubular (CFST) column subject to pure compression is determined. The dimensions of the CFST column are shown in Figure 1.

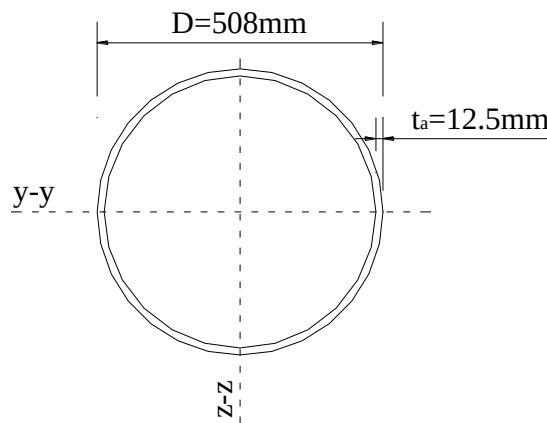


Figure 1: Cross-sectional dimensions of CFST column in Example 1

The column lengths and design loads are given as:

Column system length	$L=4000$ mm
Effective length	$L_{\text{eff}}=4000$ mm
Total design axial load	$N_{\text{Ed}}=11000$ kN
Design axial load that is permanent	$N_{\text{G,Ed}}=4500$ kN

To evaluate and compare their resistance, the following steel and concrete material grades are used:

- CHS 508x12.5 - S355 steel + C40/50 concrete
- CHS 508x12.5 - S355 steel + C90/105 concrete
- CHS 508x12.5 - S460 steel + C40/50 concrete
- CHS 406x12 - S460 steel + C90/105 concrete

1.2 CHS 508x12.5 - S355 steel tube infilled with C40/50 concrete

o Material

Concrete	C40/50, $f_{\text{ck}}=40$ N/mm ²
----------	--

Steel tube

Grade S355, $f_y=355 \text{ N/mm}^2$

o Design strengths and modulus of material

Refer to Table 2.1 and Table 2.3 of BC4 for the characteristic strength of concrete and steel, and Table 1.1 of BC4 for the partial factors, the design strengths are determined as:

$$f_{yd} = f_y / \gamma_a = 355 / 1.0 = 355 \text{ N/mm}^2$$

$$E_a = 210 \text{ GPa}$$

$$f_{cd} = f_{ck} / \gamma_c = 40 / 1.5 = 26.7 \text{ N/mm}^2$$

$$f_{cm} = f_{ck} + 8 = 40 + 8 = 48 \text{ N/mm}^2$$

$$E_{cm} = 22 (f_{cm} / 10)^{0.3} = 22 (48 / 10)^{0.3} = 35.2 \text{ GPa}$$

o Cross sectional areas

$$A_a = (\pi/4) [D^2 - (D - 2t)^2] = (\pi/4) [508^2 - (508 - 2 \times 12.5)^2] = 19458 \text{ mm}^2$$

$$A_c = (\pi/4) (D - 2t)^2 = (\pi/4) (508 - 2 \times 12.5)^2 = 183225 \text{ mm}^2$$

Unless otherwise stated, the subscript “a” stands for the steel section, and the “c” stands for the concrete section.

o Second moment of areas

$$I_a = (\pi/64) [D^4 - (D - 2t)^4] = (\pi/64) [508^4 - (508 - 2 \times 12.5)^4] \times 10^{-4} = 59755 \text{ cm}^4$$

$$I_c = (\pi/64) (D - 2t)^4 = (\pi/64) (508 - 2 \times 12.5)^4 \times 10^{-4} = 267152 \text{ cm}^4$$

o Check for local buckling (refer to Table 3.1 of BC4)

$$D/t_a = 508/12.5 = 40.6 < 90 (235/f_y) = 90 (235/355) = 59.6$$

Resistance against local buckling is adequate!

o Long-term effect

The long-term effect could be evaluated in accordance with EN 1992-1-1: 2004. Herein, the simplified method given in guidebook by Liew and Xiong (2015) “Design Guide for Concrete Filled Tubular Members with High Strength Materials – An Extension of Eurocode 4 Method to C90/105 Concrete and S550 Steel” is referred to.

The age of concrete at the moment considered t is conservatively taken as infinity. For the age of concrete on first loading by effects of creep, although EN 1994-1-1 (2004) recommends $t_0 = 1$ day, it is actually the judgement of designer to determine t_0 since it makes quite a difference whether this age is assumed to be 1 day or 1 month. Herein, t_0 is assumed as 14 days, as said, it could be different. The relative humidity RH for infilled concrete is taken as 50%.

$$\text{Perimeter of concrete section: } u = \pi(D - 2t_a) = \pi(508 - 2 \times 12.5) = 1517 \text{ mm}$$

$$\text{Notional size of concrete section: } h_0 = 2A_c/u = 2 \times 183225/1517.4 = 241.5 \text{ mm}$$

$$\text{Coefficient: } \alpha_1 = (35/f_{cm})^{0.7} = (35/48)^{0.7} = 0.80$$

$$\text{Coefficient: } \alpha_2 = (35/f_{cm})^{0.2} = (35/48)^{0.2} = 0.94$$

$$\text{Coefficient: } \alpha_3 = (35/f_{cm})^{0.5} = (35/48)^{0.5} = 0.85$$

$$\text{Factor: } \varphi_{RH} = \left(1 + \frac{1 - RH/100}{0.1\sqrt[3]{h_0}} \alpha_1 \right) \alpha_2 = \left(1 + \frac{1 - 50/100}{0.1\sqrt[3]{241.5}} \times 0.80 \right) \times 0.94 = 1.54$$

$$\text{Factor: } \beta(f_{cm}) = 16.8/\sqrt{f_{cm}} = 16.8/\sqrt{48} = 2.42$$

$$\text{Factor: } \beta(t_0) = 1/(0.1 + t_0^{0.2}) = 1/(0.1 + 14^{0.2}) = 0.56$$

$$\text{Factor: } \varphi_0 = \varphi_{RH} \beta(f_{cm}) \beta(t_0) = 1.54 \times 2.42 \times 0.56 = 2.08$$

$$\begin{aligned} \text{Factor: } \beta_H &= 1.5 \left[1 + (0.012RH)^{18} \right] h_0 + 250\alpha_3 \\ &= 1.5 \left[1 + (0.012 \times 50)^{18} \right] \times 241.5 + 250 \times 0.85 = 576 \end{aligned}$$

$$\text{Factor: } \beta_c(t, t_0) = \left(\frac{t - t_0}{\beta_H + t - t_0} \right)^{0.3} = \left(\frac{\infty - 14}{576 + \infty - 14} \right)^{0.3} = 1.0$$

$$\text{Creep coefficient: } \varphi_t = \varphi_0 \beta_c(t, t_0) = 2.08 \times 1.0 = 2.08$$

- o Elastic modulus of concrete considering long-term effect (refer to Eq.(3.14) of BC4)

Concrete is sensitive to long-term deformations due to creep and shrinkage. To allow for this, the flexural stiffness of concrete section is reduced.

$$E_{c,eff} = \frac{E_{cm}}{1 + (N_{G,Ed}/N_{Ed})\varphi_t} = \frac{35.2}{1 + (4500/11000) \times 2.08} = 19 \text{ GPa}$$

- o Effective flexural stiffness of cross-section

$$(EI)_{eff} = E_a I_a + 0.6 E_{c,eff} I_c = (210 \times 10^3 \times 59755 \times 10^4 + 0.6 \times 19 \times 10^3 \times 267152 \times 10^4) \times 10^{-3} \\ = 1.56 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

- o Elastic critical Euler buckling resistance

$$N_{cr} = \frac{\pi^2 (EI)_{eff}}{L_{eff}^2} = \frac{\pi^2 \times 1.56 \times 10^{11}}{4000^2} = 96209 \text{ kN}$$

- o Characteristic plastic resistance of cross-section

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = (19458 \times 355 + 183225 \times 40) \times 10^{-3} = 14250 \text{ kN}$$

- o Relative slenderness ratio

$$\bar{\lambda} = \sqrt{\frac{N_{pl,Rk}}{N_{cr}}} = \sqrt{\frac{14250}{96209}} = 0.385 < 0.5$$

- o Confinement coefficients with load eccentricity $e=0$

Since the slenderness $\bar{\lambda}$ is less than 0.5 and the load eccentricity is equal to 0 (axially loaded column), the confinement effect may be considered for the circular CFST column.

$$\eta_a = \eta_{a0} = \min \left[0.25(3 + 2\bar{\lambda}), 1.0 \right] = 0.942$$

$$\eta_c = \eta_{c0} = \max \left[4.9 - 18.5\bar{\lambda} + 17\bar{\lambda}^2, 0 \right] = 0.298$$

- o Design plastic resistance of cross-section considering the confinement effect (refer to Eq.(3.2) of BC4)

$$N_{pl,Rd} = \eta_a A_a f_{yd} + A_c f_{cd} \left(1 + \eta_c \frac{t}{D} \frac{f_y}{f_{ck}} \right) \\ = \left[0.942 \times 19458 \times 355 + 183225 \times 26.7 \left(1 + 0.298 \frac{12.5}{508} \frac{355}{40} \right) \right] \times 10^{-3} \\ = 11727 \text{ kN}$$

It is worthwhile to note that the yield strength of steel is reduced ($\eta_a < 0$) and strength of concrete increases ($1 + \eta_c \frac{t}{D} \frac{f_y}{f_{ck}} > 0$) with the consideration of confinement effect.

- o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = (19458 \times 10^{-3} \times 355) / 11727 = 0.59 < 0.9$$

- o Imperfection factor

Refer to Table 3.3 of BC4, the buckling curve is taken as “a”. Thus the imperfection factor α is determined as 0.21 according to Table 3.2 of BC4.

- o Buckling reduction factor

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.385 - 0.2) + 0.385^2 \right] = 0.593$$

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}} = \frac{1}{0.593 + \sqrt{0.593^2 - 0.385^2}} = 0.957$$

- o Buckling resistance

According to Section 3.3.1 of BC4, the axial buckling resistance is checked as:

$$N_{b,Rd} = \chi N_{pl,Rd} = 0.957 \times 11727 = 11223 \text{ kN} > N_{Ed} = 10000 \text{ kN}$$

Buckling resistance is adequate!

1.3 CHS 508x12.5 - S355 steel tube infilled with C90/105 concrete

In this section, the normal strength concrete (NSC) C40/50 is replaced by high strength concrete (HSC) C90/105. The steel grade is not changed.

- o Design strength

Refer to Table 2.2, Eq.(2.2) and Eq.(2.3) of BC4, the effective compressive strength and modulus of elasticity of the HSC are calculated as:

$$f_{ck} = 72 \text{ N/mm}^2$$

$$E_{cm} = 41.1 \text{ GPa}$$

$$f_{cd} = f_{ck} / \gamma_c = 72 / 1.5 = 48 \text{ N/mm}^2$$

$$f_{cm} = f_{ck} + 8 = 72 + 8 = 80 \text{ N/mm}^2$$

- o Creep coefficient could be similarly determined as $\varphi_t = 1.29$.
- o Elastic modulus of concrete considering long-term effect

$$E_{c,eff} = E_{cm} \frac{1}{1 + (N_{G,Ed} / N_{Ed}) \varphi_t} = \frac{41.1}{1 + (4500 / 11000) \times 1.29} = 26.9 \text{ GPa}$$

- o Effective flexural stiffness of cross-section

$$\begin{aligned} (EI)_{eff} &= E_a I_a + 0.6 E_{c,eff} I_c \\ &= (210 \times 10^3 \times 59755 \times 10^4 + 0.6 \times 26.9 \times 10^3 \times 267152 \times 10^4) \times 10^{-3} \\ &= 1.69 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

- o Confinement effect and design plastic resistance of cross-section

$$N_{cr} = \frac{\pi^2 (EI)_{eff}}{L_{eff}^2} = \frac{\pi^2 \times 1.69 \times 10^{11}}{4000^2} = 104010 \text{ kN}$$

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = (19458 \times 355 + 183225 \times 72) \times 10^{-3} = 20112 \text{ kN}$$

$$\bar{\lambda} = \sqrt{\frac{N_{pl,Rk}}{N_{cr}}} = \sqrt{\frac{20112}{104010}} = 0.44 < 0.5$$

$$\eta_a = \eta_{a0} = \min \left[0.25 (3 + 2\bar{\lambda}), 1.0 \right] = 0.970$$

$$\eta_c = \eta_{c0} = \max \left[4.9 - 18.5\bar{\lambda} + 17\bar{\lambda}^2, 0 \right] = 0.052$$

$$\begin{aligned} N_{pl,Rd} &= \eta_a A_a f_{yd} + A_c f_{cd} \left(1 + \eta_c \frac{t}{D} \frac{f_y}{f_{ck}} \right) \\ &= \left[0.970 \times 19458 \times 355 + 183225 \times 48 \left(1 + 0.052 \frac{12.5}{508} \frac{355}{72} \right) \right] \times 10^{-3} = 15562 \text{ kN} \end{aligned}$$

- o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = (19458 \times 10^{-3} \times 355) / 15562 = 0.444 < 0.9$$

o Buckling resistance

Buckling curve="a", $\alpha=0.21$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.44 - 0.2) + 0.44^2 \right] = 0.622$$

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}} = \frac{1}{0.622 + \sqrt{0.622^2 - 0.44^2}} = 0.942$$

Thus, the axial buckling resistance is:

$$N_{b,Rd} = \chi N_{pl,Rd} = 0.942 \times 15562 = 14659 \text{ kN}$$

Compared with that using NSC C40/50, the buckling resistance is increased by:

$$\frac{14659 - 11223}{11223} \times 100\% = 30.6\%$$

By replacing C40/50 normal strength concrete with C90/105 high strength concrete, the axial buckling resistance of the CFST column is improved by 31%.

1.4 CHS 508x12.5 - S460 steel tube infilled with C40/50 concrete

In this section, the mild steel S355 is replaced by S460, the concrete grade is not changed.

o Confinement effect and design plastic resistance of cross-section

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = (19458 \times 460 + 183225 \times 40) \times 10^{-3} = 16297 \text{ kN}$$

$$\bar{\lambda} = \sqrt{\frac{N_{pl,Rk}}{N_{cr}}} = \sqrt{\frac{16297}{96209}} = 0.412 < 0.5$$

$$\eta_a = \eta_{a0} = \min \left[0.25 (3 + 2\bar{\lambda}), 1.0 \right] = 0.956$$

$$\eta_c = \eta_{c0} = \max \left[4.9 - 18.5\bar{\lambda} + 17\bar{\lambda}^2, 0 \right] = 0.166$$

$$\begin{aligned} N_{pl,Rd} &= \eta_a A_a f_{yd} + A_c f_{cd} \left(1 + \eta_c \frac{t}{D} \frac{f_y}{f_{ck}} \right) \\ &= \left[0.956 \times 19458 \times 355 + 183225 \times 26.7 \left(1 + 0.166 \frac{12.5}{508} \frac{355}{40} \right) \right] \times 10^{-3} \\ &= 13687 \text{ kN} \end{aligned}$$

- o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = (19458 \times 10^{-3} \times 460) / 13687 = 0.655$$

- o Buckling resistance

Buckling curve="a", $\alpha=0.21$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.412 - 0.2) + 0.412^2 \right] = 0.607$$

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}} = \frac{1}{0.607 + \sqrt{0.607^2 - 0.412^2}} = 0.95$$

$$N_{b,Rd} = \chi N_{pl,Rd} = 0.95 \times 13687 = 13003 \text{ kN}$$

Compared with that with the mild steel S355, the axial buckling resistance by using S460 is increased by:

$$\frac{13003 - 11223}{11223} \times 100\% = 15.9\%$$

By use of steel S460 replacing S355, the axial buckling resistance of the CFST column is improved by 15.9%.

1.5 CHS 406x12 - S460 steel tube infilled C90/105 concrete

In this section, the normal strength materials are replaced by higher strength steel S460 and concrete C90/105. The compatibility between steel grade and concrete class should be evaluated in accordance with Table 2.7 of BC4. The purpose of using higher strength materials is to reduce the cross-sectional size of the original CFST column but the axial buckling resistance remains the same.

- o CHS 406x12 with S460 steel is tried

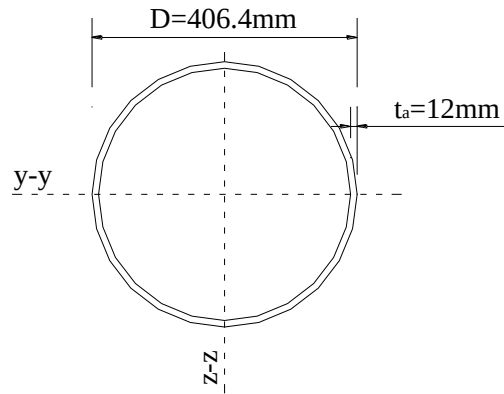


Figure 2: Reduced cross-sectional size

o Section properties

$$A_a = (\pi/4) [D^2 - (D - 2t)^2] = (\pi/4) [406.4^2 - (406.4 - 2 \times 12)^2] = 14900 \text{ mm}^2$$

$$A_c = (\pi/4) (D - 2t)^2 = (\pi/4) (406.4 - 2 \times 12)^2 = 114800 \text{ mm}^2$$

$$I_a = (\pi/64) [D^4 - (D - 2t)^4] = (\pi/64) [406.4^4 - (406.4 - 2 \times 12)^4] \times 10^{-4} = 28940 \text{ cm}^4$$

$$I_c = (\pi/64) (D - 2t)^4 = (\pi/64) (406.4 - 2 \times 12)^4 \times 10^{-4} = 104961 \text{ cm}^4$$

o Effective flexural stiffness of cross-section

Creep coefficient is similarly determined as $\varphi_t = 1.32$

$$E_{c,eff} = \frac{E_{cm}}{1 + (N_{G,Ed} / N_{Ed}) \varphi_t} = \frac{41.1}{1 + (4500/11000) \times 1.32} = 26.7 \text{ GPa}$$

$$\begin{aligned} (EI)_{eff} &= E_a I_a + 0.6 E_{c,eff} I_c \\ &= (210 \times 10^3 \times 28940 \times 10^4 + 0.6 \times 26.7 \times 10^3 \times 104961 \times 10^4) \times 10^{-3} \\ &= 7.76 \times 10^{10} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

o Confinement effect and design plastic resistance of cross-section

$$N_{cr} = \frac{\pi^2 (EI)_{eff}}{L_{eff}^2} = \frac{\pi^2 \times 7.76 \times 10^{10}}{4000^2} = 47849 \text{ kN}$$

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = (14900 \times 460 + 114800 \times 72) \times 10^{-3} = 15121 \text{ kN}$$

$$\bar{\lambda} = \sqrt{\frac{N_{pl,Rk}}{N_{cr}}} = \sqrt{\frac{15121}{47849}} = 0.562 > 0.5$$

Since the relative slenderness ratio is higher than 0.5, the confinement effect is not taken into account, thus

$$N_{pl,Rd} = A_a f_{yd} + A_c f_{cd} = (14900 \times 460 + 114800 \times 48) \times 10^{-3} = 12365 \text{ kN}$$

o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = (14900 \times 10^{-3} \times 460) / 12365 = 0.554 < 0.9$$

o Buckling resistance

Buckling curve "a" is used, imperfection factor $\alpha=0.21$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.562 - 0.2) + 0.562^2 \right] = 0.696$$

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}} = \frac{1}{0.696 + \sqrt{0.696^2 - 0.562^2}} = 0.904$$

The axial buckling resistance is:

$$N_{b,Rd} = \chi N_{pl,Rd} = 0.904 \times 12365 = 11178 \text{ kN}$$

Thus, the buckling resistance is almost the same as the CHS 508x12.5 - S355 steel with C40/50 concrete infilled as calculated in Section 1.2.

o Reductions of sectional and surface area

The column section area is thus reduced by

$$\frac{\Delta A_f}{A_f} = \frac{\pi/4 \times (508^2 - 406.4^2)}{\pi/4 \times 508^2} = 36\%$$

The surface area of the column is reduced by

$$\frac{\Delta A_s}{A_s} = \frac{\pi \times (508 - 406.4)}{\pi \times 508} = 20\%$$

With the reduced surface area, the cost of fire protection material may be reduced since the labour cost for applying the fire protection material is based on the surface area. In

addition, welding work and labour cost will be reduced as the less construction materials are needed for smaller column size.

1.6 Summary

For CFST columns subject to axial compression force only (mainly used in braced frames with simple construction), the use of high strength concrete will benefit more than the use of higher grade steels, compared with the increase of cost.

With the use of high strength materials, the column size is reduced. As a result, the fabrication cost of column and labour cost for applying fire protection are reduced, and the usable floor area is increased.

2 Example 2

2.1 General

In Example 2, the design resistance of a circular concrete filled steel tubular member with encased reinforcements and UC steel section is checked against combined compression and uniaxial bending moment about the major axis. The dimensions of the CFST column are shown in Figure 3.

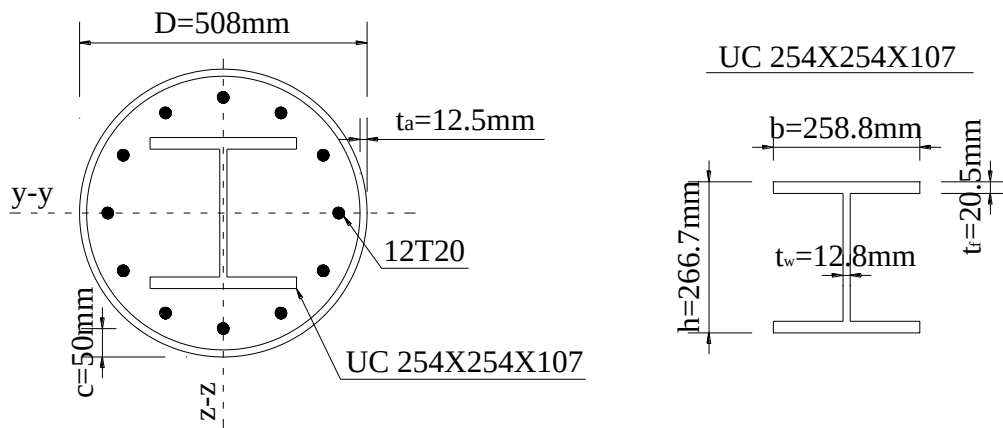
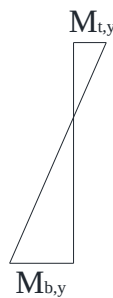


Figure 3: Cross-sectional dimensions of CFST column in Example 2

The column lengths and design loads are given as:

Column system length	$L=4000$ mm
Effective length	$L_{\text{eff}}=4000$ mm
Total design axial load	$N_{\text{Ed}}=10000$ kN
Design axial load that is permanent	$N_{\text{G,Ed}}=4000$ kN



Design moment at bottom around y-y axis	$M_{\text{b,y}}=700$ kN.m
Design moment at top around y-y axis	$M_{\text{t,y}}=-500$ kN.m

To evaluate the resistance, the following steel, concrete and reinforcing steel are used:

- a) CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C50/60 concrete and G460 reinforcements
- b) CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C90/105 concrete and G460 reinforcements
- c) CHS 508x12.5 and UC 254x254x107 - S500 steel sections with C50/60 concrete and G460 reinforcements

2.2 CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C50/60 concrete and G460 reinforcements

○ Material

Concrete	C50/60, $f_{ck}=50 \text{ N/mm}^2$
Steel tube	Grade S355, $f_y=355 \text{ N/mm}^2$
Embedded steel section	Grade S355, $f_{ek}=355 \text{ N/mm}^2$
Reinforcements	Grade 460, $f_{sk}=460 \text{ N/mm}^2$

○ Design strength and modulus of material

Unless otherwise stated, the subscript “e” stands for the encased steel section, and the “s” stands for the reinforcing steel.

$$f_{yd} = f_y / \gamma_a = 355 / 1.0 = 355 \text{ N/mm}^2$$

$$f_{sd} = f_{sk} / \gamma_s = 460 / 1.15 = 400 \text{ N/mm}^2$$

$$f_{ed} = f_{ek} / \gamma_a = 355 / 1.0 = 355 \text{ N/mm}^2$$

$$f_{cd} = f_{ck} / \gamma_c = 50 / 1.5 = 33.3 \text{ N/mm}^2$$

$$f_{cm} = f_{ck} + 8 = 50 + 8 = 58 \text{ N/mm}^2$$

$$E_a = E_s = E_e = 210 \text{ GPa}$$

$$E_{cm} = 22 (f_{cm} / 10)^{0.3} = 22 (58 / 10)^{0.3} = 37.3 \text{ GPa}$$

○ Cross sectional areas

$$A = (\pi/4) D^2 = (\pi/4) \times 508^2 = 202683 \text{ mm}^2$$

$$A_a = (\pi/4) [D^2 - (D - 2t_a)^2] = (\pi/4) [508^2 - (508 - 2 \times 12.5)^2] = 19458 \text{ mm}^2$$

$$A_e = bh - (b - t_w)(h - 2t_f)$$

$$= 258.8 \times 266.7 - (258.8 - 12.8)(266.7 - 2 \times 20.5) = 13500 \text{ mm}^2$$

$$A_s = 12 \left(\frac{\pi}{4} \right) d^2 = 12 \times \left(\frac{\pi}{4} \right) \times 20^2 = 3770 \text{ mm}^2$$

$$A_c = A - A_a - A_e - A_s = 202683 - 19458 - 13500 - 3770 = 165955 \text{ mm}^2$$

○ Second moment of areas

For simplicity, the reinforcements are equivalently converted to a circular tube based on the same cross-sectional area and position of centreline, as shown in Figure 4.

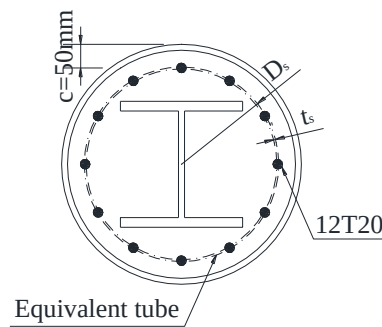


Figure 4: Equivalent tube section for reinforcing steel

$$t_s = \frac{A_s}{\pi(D - 2c)} = \frac{3770}{\pi \times (508 - 2 \times 50)} = 2.94 \text{ mm}$$

$$D_s = D - 2c + t_s = 508 - 2 \times 50 + 2.94 = 410.9 \text{ mm}$$

$$I = \left(\frac{\pi}{64} \right) D^4 = \left(\frac{\pi}{64} \right) \times 508^4 \times 10^{-4} = 326907 \text{ cm}^4$$

$$\begin{aligned} I_a &= \left(\frac{\pi}{64} \right) \left[D^4 - (D - 2t_a)^4 \right] \\ &= \left(\frac{\pi}{64} \right) \left[508^4 - (508 - 2 \times 12.5)^4 \right] \times 10^{-4} = 59755 \text{ cm}^4 \end{aligned}$$

$$\begin{aligned} I_s &= \left(\frac{\pi}{64} \right) \left[D_s^4 - (D_s - 2t_s)^4 \right] \\ &= \left(\frac{\pi}{64} \right) \left[410.9^4 - (410.9 - 2 \times 2.94)^4 \right] \times 10^{-4} = 7840 \text{ cm}^4 \end{aligned}$$

$$\begin{aligned} I_{ey} &= \frac{1}{12} \left[bh^3 - (b - t_w)(h - 2t_f)^3 \right] \\ &= \frac{1}{12} \left[258.8 \times 266.7^3 - (258.8 - 12.8)(266.7 - 2 \times 20.5)^3 \right] \times 10^{-4} = 17343 \text{ cm}^4 \end{aligned}$$

$$I_{ez} = \frac{1}{12} \left[2t_f b^3 + (h - 2t_f) t_w^3 \right]$$

$$= \frac{1}{12} \left[2 \times 20.5 \times 258.8^3 + (266.7 - 2 \times 20.5) \times 12.8^3 \right] \times 10^{-4} = 5926 \text{ cm}^4$$

$$I_{cy} = I - I_a - I_s - I_{ey} = 326907 - 59755 - 7840 - 17343 = 241969 \text{ cm}^4$$

$$I_{cz} = I - I_a - I_s - I_{ez} = 326907 - 59755 - 7840 - 5926 = 253386 \text{ cm}^4$$

○ Plastic modulus

$$W = D^3/6 = 508^3/6 \times 10^{-3} = 21850 \text{ cm}^3$$

$$W_a = \left[D^3 - (D - 2t_a)^3 \right] / 6 = \left[508^3 - (508 - 2 \times 12.5)^3 \right] / 6 \times 10^{-3} = 3070 \text{ cm}^3$$

$$W_s = \left[D_s^3 - (D_s - 2t_s)^3 \right] / 6 = \left[410.9^3 - (410.9 - 2 \times 2.94)^3 \right] / 6 \times 10^{-3} = 489 \text{ cm}^3$$

$$W_{ey} = \frac{1}{4} \left[b h^2 - (b - t_w) (h - 2t_f)^2 \right]$$

$$= \frac{1}{4} \left[258.8 \times 266.7^2 - (258.8 - 12.8) (266.7 - 2 \times 20.5)^2 \right] \times 10^{-3} = 1469 \text{ cm}^3$$

$$W_{ez} = \frac{1}{4} \left[2t_f b^2 + (h - 2t_f) t_w^2 \right]$$

$$= \frac{1}{4} \left[2 \times 20.5 \times 258.8^2 + (266.7 - 2 \times 20.5) \times 12.8^2 \right] \times 10^{-4} = 696 \text{ cm}^4$$

$$W_{cy} = W - W_a - W_s - W_{ey} = 21850 - 3070 - 489 - 1469 = 16821 \text{ cm}^4$$

$$W_{cz} = W - W_a - W_s - W_{ez} = 21850 - 3070 - 489 - 696 = 17594 \text{ cm}^4$$

○ Check for local buckling

$$D/t_a = 508/12.5 = 40.6 < 90(235/f_y) = 90(235/355) = 59.6$$

Resistance against local buckling is adequate!

○ Long-term effect

Age of concrete at loading in days: $t_0 = 30$

Age of concrete at moment considered in days: $t = \infty$

Relative humidity of ambient environment: RH=50%

Perimeter of concrete section: $u = \pi(D - 2t_a) = \pi(508 - 2 \times 12.5) = 1517 \text{ mm}$

Notional size of concrete section: $h_0 = 2A_c/u = 2 \times 165955/1517 = 219 \text{ mm}$

Coefficient: $\alpha_1 = (35/f_{cm})^{0.7} = (35/58)^{0.7} = 0.70$

Coefficient: $\alpha_2 = (35/f_{cm})^{0.2} = (35/58)^{0.2} = 0.90$

Coefficient: $\alpha_3 = (35/f_{cm})^{0.5} = (35/58)^{0.5} = 0.78$

Factor: $\varphi_{RH} = \left(1 + \frac{1 - RH/100}{0.1\sqrt[3]{h_0}} \alpha_1\right) \alpha_2 = \left(1 + \frac{1 - 50/100}{0.1\sqrt[3]{219}} \times 0.70\right) \times 0.90 = 1.43$

Factor: $\beta(f_{cm}) = 16.8/\sqrt{f_{cm}} = 16.8/\sqrt{58} = 2.21$

Factor: $\beta(t_0) = 1/(0.1 + t_0^{0.2}) = 1/(0.1 + 30^{0.2}) = 0.48$

Factor: $\varphi_0 = \varphi_{RH} \beta(f_{cm}) \beta(t_0) = 1.43 \times 2.21 \times 0.48 = 1.52$

Factor: $\beta_H = 1.5 \left[1 + (0.012RH)^{18}\right] h_0 + 250\alpha_3$
 $= 1.5 \times \left[1 + (0.012 \times 50)^{18}\right] \times 219 + 250 \times 0.78 = 522$

Factor: $\beta_c(t, t_0) = \left(\frac{t - t_0}{\beta_H + t - t_0}\right)^{0.3} = \left(\frac{\infty - 14}{522 + \infty - 14}\right)^{0.3} = 1.0$

Creep coefficient: $\varphi_t = \varphi_0 \beta_c(t, t_0) = 1.52 \times 1.0 = 1.52$

- Elastic modulus of concrete considering long-term effect

$$(1) E_{c,eff} = E_{cm} \frac{1}{1 + (N_{G,Ed}/N_{Ed}) \varphi_t} = \frac{37.3}{1 + (4000/10000) \times 1.52} = 23.2 \text{ GPa}$$

- Effective flexural stiffness of cross-section

$$(EI)_{eff,y} = E_a I_a + E_s I_s + E_e I_{ey} + 0.6 E_{c,eff} I_{cy}$$

$$= [210 \times (59755 + 7840 + 17343) + 0.6 \times 23.2 \times 241969] \times 10^4$$

$$= 2.12 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

$$(EI)_{eff,z} = E_a I_a + E_s I_s + E_e I_{ez} + 0.6 E_{c,eff} I_{cz}$$

$$= [210 \times (59755 + 7840 + 5926) + 0.6 \times 23.2 \times 253386] \times 10^4$$

$$= 1.90 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

- Elastic critical Euler buckling resistance

$$N_{cr,y} = \frac{\pi^2 (EI)_{eff,y}}{L_{eff}^2} = \frac{\pi^2 \times 2.12 \times 10^{11}}{4000^2} = 130793 \text{ kN}$$

$$N_{cr,z} = \frac{\pi^2 (EI)_{eff,z}}{L_{eff}^2} = \frac{\pi^2 \times 1.90 \times 10^{11}}{4000^2} = 116984 \text{ kN}$$

- Characteristic plastic resistance of cross-section

$$\begin{aligned} N_{pl,Rk} &= A_a f_y + A_s f_{sk} + A_e f_{ek} + A_c f_{ck} \\ &= [(19458 + 13500) \times 355 + 3770 \times 460 + 165955 \times 50] \times 10^{-3} = 21475 \text{ kN} \end{aligned}$$

- Relative slenderness ratio

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{21475}{130793}} = 0.408 < 0.5$$

$$\bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{21475}{116984}} = 0.431 < 0.5$$

- Buckling curves and buckling reduction factors

Since a steel section is embedded in the CFST column, the buckling curves about both axis are “b”. Thus, the imperfection factor is $\alpha = 0.34$.

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.431$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.34 \times (0.431 - 0.2) + 0.431^2 \right] = 0.632$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.632 + \sqrt{0.632^2 - 0.431^2}}, 1.0 \right) = 0.914$$

- Load eccentricity

$$e_{N,y} = \frac{\max(|M_{t,y}|, |M_{b,y}|)}{N_{Ed}} = \frac{700}{10000} \times 10^3 = 70 \text{ mm} > 0.1D = 50.8 \text{ mm}$$

Since the eccentricity $e_{N,y}$ is larger than $0.1D$, the confinement effect is not taken into account.

○ Simplified Interaction Curve

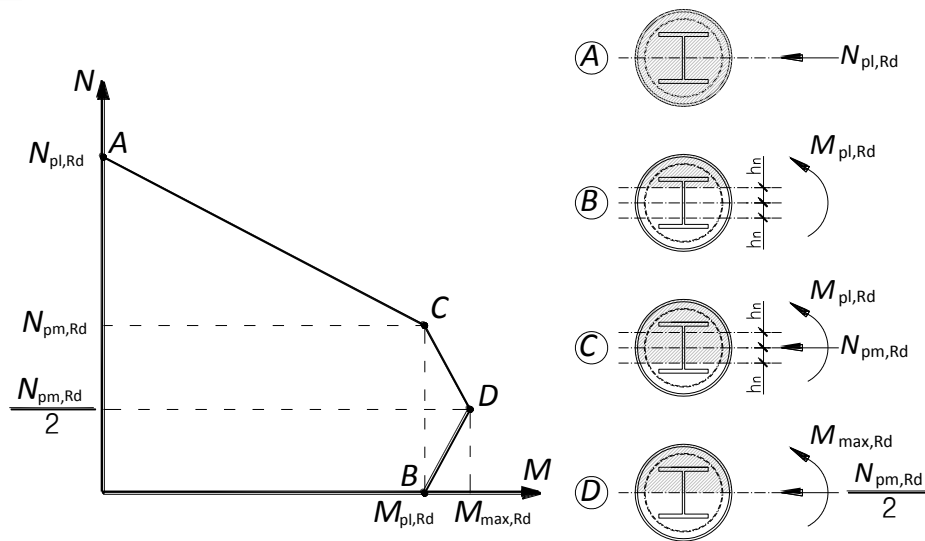


Figure 5: Simplified interaction curve for circular CFST column with encased steel section

1) Point A (0, $N_{pl,Rd}$):

Full cross-section is under uniform compression. No bending moment is resultant from the compressive stresses on the cross-section.

$$\begin{aligned}
 N_{pl,Rd} &= A_a f_{yd} + A_s f_{sd} + A_e f_{ed} + A_c f_{cd} \\
 &= [(19458 + 13500) \times 355 + 3770 \times 400 + 165955 \times 33.3] \times 10^{-3} \\
 &= 18753 \text{ kN}
 \end{aligned}$$

2) Point B ($M_{pl,Rd}$, 0):

The cross-section is under partial compression and no axial force is formed. Assuming the neutral axis lies in the web of encased section ($h_n \leq h/2 - t_f$), the height of neutral axis is calculated where the areas of steel tube, equivalent tube for reinforcements, and concrete in the height of $2h_n$ are approximated as rectangles, and based on the force equilibrium between the tensile capacity of steel sections within the height of $2h_n$ is equal to the compression resistance of concrete in the compression zone. Unless otherwise stated, the tensile resistance of concrete in the tension zone is conservatively ignored.

$$\begin{aligned}
 h_n &= \frac{A_c f_{cd}}{2Df_{cd} + 4t_a(2f_{yd} - f_{cd}) + 4t_s(2f_{sd} - f_{cd}) + 2t_w(2f_{ed} - f_{cd})} \\
 &= \frac{165955 \times 33.3}{2 \times 508 \times 33.3 + 4 \times 12.5 \times (2 \times 355 - 33.3) + 4 \times 2.94 \times (2 \times 400 - 33.3) + 2 \times 12.8 \times (2 \times 355 - 33.3)} \\
 &= 58.8 \text{ mm}
 \end{aligned}$$

$$h_n = 58.8 \text{ mm} < h/2 - t_f = 266.7/2 - 20.5 = 112.85 \text{ mm}$$

Thus, the neutral axial lies in the web of the encased section. The plastic modulus of steel tube, equivalent tube of reinforcements, encased section, and concrete in the height of $2h_n$, bending about centreline of the cross-section are calculated as:

$$W_{a,n} = 2t_a h_n^2 = 2 \times 12.5 \times 58.8^2 \times 10^{-3} = 86.4 \text{ cm}^3$$

$$W_{s,n} = 2t_s h_n^2 = 2 \times 2.94 \times 58.8^2 \times 10^{-3} = 20.3 \text{ cm}^3$$

$$W_{ey,n} = t_w h_n^2 = 12.8 \times 58.8^2 \times 10^{-3} = 44.3 \text{ cm}^3$$

$$W_{cy,n} = (D - 2t_a - 2t_s - t_w) h_n^2 = (508 - 2 \times 12.5 - 2 \times 2.94 - 12.8) \times 58.8^2 \times 10^{-3} = 1605 \text{ cm}^3$$

Taking moment about the centreline of the cross-section, the plastic bending resistance is determined from:

$$\begin{aligned}
 M_{pl,Rd} &= (W_a - W_{a,n}) f_{yd} + (W_s - W_{s,n}) f_{sd} + (W_{ey} - W_{ey,n}) f_{ed} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\
 &= [(3070 - 86.4) \times 355 + (489 - 20.3) \times 400 + (1469 - 44.3) \times 355 + 0.5 \times (16821 - 1605) \times 33.3] \times 10^{-3} \\
 &= 2006 \text{ kN} \cdot \text{m}
 \end{aligned}$$

It should be noted that the plastic bending resistance can be calculated by taking moment about either line on the cross-section parallel to the y-y axis, as long as the aforementioned plastic modulus are determined according to the referred line.

3) Point C ($M_{pl,Rd}$, $N_{pm,Rd}$):

The cross-section is under partial compression but axial force is resultant from the compressive stresses. The axial force is equal to the compression capacities of concrete in the compression zone and steel sections within the height of $2h_n$. It is mentioned above that the compression capacity of steel sections within the height of $2h_n$ is equal to the compression capacity of concrete in the compression zone and out of the height of $2h_n$.

Thus, the axial force is actually the full cross-sectional compression capacity of concrete and determined from:

$$N_{pm,Rd} = A_c f_{cd} = 165955 \times 33.3 \times 10^{-3} = 5526 \text{ kN}$$

4) Point D ($M_{\max,Rd}$, $N_{pm,Rd}/2$):

The maximum plastic moment resistance $M_{\max,Rd}$ is calculated when the h_n is equal to 0.

$$\begin{aligned} M_{\max,Rd} &= W_a f_{yd} + W_s f_{sd} + W_{ey} f_{ed} + 0.5 W_{cy} f_{cd} \\ &= [3070 \times 355 + 489 \times 400 + 1469 \times 355 + 0.5 \times 16821 \times 33.3] \times 10^{-3} = 2087 \text{ kN} \cdot \text{m} \end{aligned}$$

- Steel contribution ratio

$$\begin{aligned} \delta &= (A_a f_{yd} + A_e f_{ed}) / N_{pl,Rd} \\ &= (19458 + 13500) \times 355 \times 10^{-3} / 18753 = 0.625 < 0.9 \end{aligned}$$

- Check for resistance of column in axial compression

$$\frac{N_{Ed}}{\chi N_{pl,Rd}} = \frac{10000}{0.914 \times 18753} = \frac{10000}{17140} = 0.583 < 1.0$$

Thus, the buckling resistance under axial compression is adequate!

- Effective flexural stiffness considering long-term effect

$$\begin{aligned} (EI)_{eff,II} &= K_0 (E_a I_a + E_s I_s + E_e I_{ey} + K_{e,II} E_{c,m} I_{cy}) \\ &= 0.9 \times [210 \times (59755 + 7840 + 17343) + 0.5 \times 23.2 \times 241969] \times 10^4 \\ &= 1.86 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

- Critical normal force about y-y axis

The effective length is taken as the system length of column.

$$N_{cr,eff} = \frac{\pi^2 (EI)_{eff,II}}{L^2} = \frac{\pi^2 \times 1.86 \times 10^{11}}{4000^2} = 114601 \text{ kN}$$

- Second-order effect (refer to Clause 3.3.2 (2) of BC4)

The second-order effect should be considered for both moments from first-order analysis and moment from imperfection as shown in Figure 6.

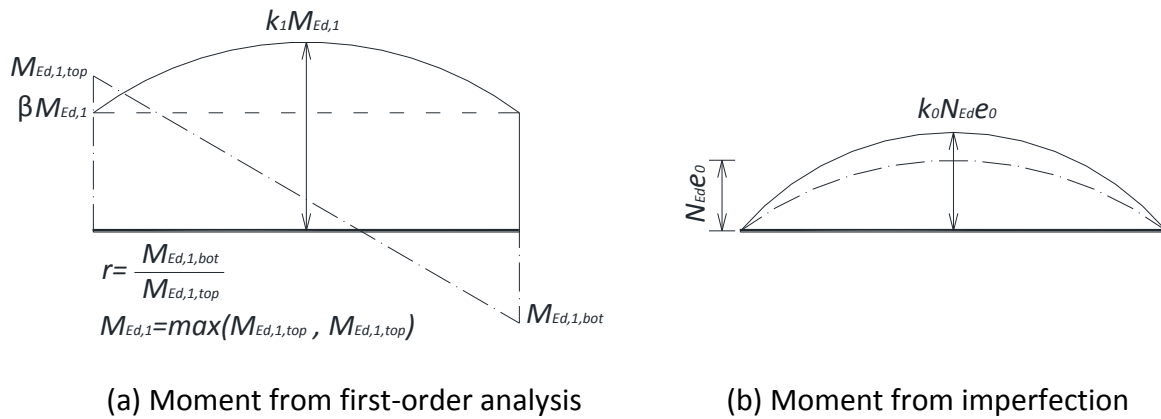


Figure 6: Consideration for second order effect

According to buckling curve “b”, the initial imperfection about y-y axial is:

$$e_{0,y} = L/200 = 4000/200 = 20 \text{ mm}$$

Accordingly, the bending moment by the initial imperfection is determined as:

$$M_0 = N_{Ed}e_{0,y} = 10000 \times 20/1000 = 200 \text{ kN} \cdot \text{m}$$

According to the moment diagram by the initial imperfection, the factor β_0 for determination of moment to second-order effect is equal to 1.0. Thus, the amplification factor for the moment by the imperfection is calculated from:

$$k_0 = \frac{\beta_0}{1 - N_{Ed}/N_{cr,eff}} = \frac{1.0}{1 - 10000/114601} = 1.096$$

According to the first-order design moment diagram, the ratio of end moments is calculated as:

$$r = M_{t,y}/M_{b,y} = -500/700 = -0.714$$

Thus, the factor β_1 for determination of moment to second-order effect is determined:

$$\beta_1 = \max(0.66 + 0.44r, 0.44) = \max(0.66 + 0.44 \times (-0.714), 0.44) = 0.44$$

Thus, the amplification factor for the moment by the imperfection is calculated from:

$$k_1 = \frac{\beta_1}{1 - N_{Ed}/N_{cr,eff}} = \frac{0.44}{1 - 10000/114601} = 0.482$$

Thus, the design moment, considering second-order effect, is calculated as:

$$\begin{aligned}
 M_{Ed} &= \text{Max} \left[k_0 M_0 + k_1 \text{Max}(|M_{t,y}|, |M_{b,y}|), \text{Max}(|M_{t,y}|, |M_{b,y}|) \right] \\
 &= \text{Max} \left[1.096 \times 200 + 0.482 \times \text{Max}(|-500|, |700|), \text{Max}(|-500|, |700|) \right] = 700 \text{ kN} \cdot \text{m}
 \end{aligned}$$

In this case, the second-order effect is not significant and the maximum end moment is taken as the design moment.

- Check for resistance of column in combined compression and uniaxial bending

For $N_{Ed} > N_{pm,Rd} = 5526 \text{ kN}$, the value for determining the plastic bending resistance $M_{pl,N,Rd}$ taking into account the normal force N_{Ed} is calculated from:

$$\mu_d = \frac{N_{pl,Rd} - N_{Ed}}{N_{pl,Rd} - N_{pm,Rd}} = \frac{18753 - 10000}{18753 - 5526} = 0.662 \text{ (refer to Eq.(3.24) of BC4)}$$

$$\frac{M_{Ed}}{M_{pl,N,Rd}} = \frac{M_{Ed}}{\mu_d M_{pl,Rd}} = \frac{700}{0.662 \times 2006} = 0.527 < \alpha_M = 0.9$$

Thus, the resistance for combined axial compression and uniaxial bending is adequate. The external design force and bending moment, and the design M-N interaction curve are plotted in Figure 7.

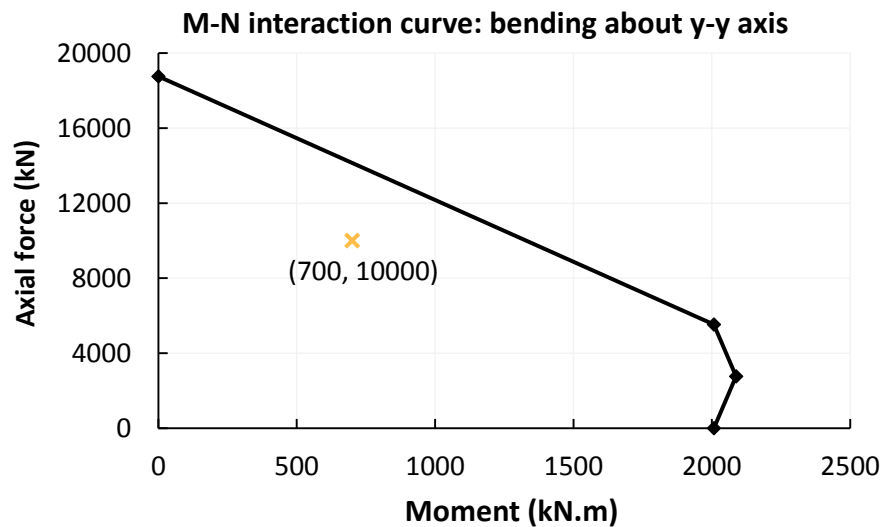


Figure 7: Design M-N interaction curve of circular CFST column

2.3 CHS 508x12.5 and UC 254x254x107 - S355 steel sections with C90/105 concrete and G460 reinforcements

In this section, the normal strength concrete (NSC) C40/50 is replaced by high strength concrete (HSC) C90/105. The steel grade is not changed.

- Design strength

Effective compressive strength and modulus of elasticity of the HSC are taken from Table 2.2, Eq.(2.2) and Eq.(2.3) of BC4.

$$f_{ck} = 72 \text{ N/mm}^2; E_{cm} = 41.1 \text{ GPa}$$

$$f_{cd} = f_{ck} / \gamma_c = 72 / 1.5 = 48 \text{ N/mm}^2$$

$$f_{cm} = f_{ck} + 8 = 72 + 8 = 80 \text{ N/mm}^2$$

- Effective flexural stiffness of cross-section

Creep coefficient could be similarly determined as $\varphi_t = 1.12$

$$E_{c,eff} = \frac{E_{cm}}{1 + (N_{G,Ed} / N_{Ed}) \varphi_t} = \frac{41.1}{1 + (4000 / 10000) \times 1.12} = 28.3 \text{ GPa}$$

$$\begin{aligned} (EI)_{eff,y} &= E_a I_a + E_s I_s + E_e I_{ey} + 0.6 E_{c,eff} I_{cy} \\ &= [210 \times (59755 + 7840 + 17343) + 0.6 \times 28.3 \times 241969] \times 10^4 \\ &= 2.19 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

$$\begin{aligned} (EI)_{eff,z} &= E_a I_a + E_s I_s + E_e I_{ez} + 0.6 E_{c,eff} I_{cz} \\ &= [210 \times (59755 + 7840 + 5926) + 0.6 \times 28.3 \times 253386] \times 10^4 \\ &= 1.97 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

- Characteristic plastic resistance of cross-section

$$N_{cr,y} = \frac{\pi^2 (EI)_{eff,y}}{L_{eff}^2} = \frac{\pi^2 \times 2.19 \times 10^{11}}{4000^2} = 135397 \text{ kN}$$

$$N_{cr,z} = \frac{\pi^2 (EI)_{eff,z}}{L_{eff}^2} = \frac{\pi^2 \times 1.97 \times 10^{11}}{4000^2} = 121805 \text{ kN}$$

$$\begin{aligned} N_{pl,Rk} &= A_a f_y + A_s f_{sk} + A_e f_{ek} + A_c f_{ck} \\ &= [(19458 + 13500) \times 355 + 3770 \times 460 + 165955 \times 90] \times 10^{-3} = 25395 \text{ kN} \end{aligned}$$

- Relative slenderness ratio, buckling curves and buckling reduction factors

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{25395}{135397}} = 0.433 < 0.5; \bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{25395}{121805}} = 0.457 < 0.5$$

For buckling curves about both axis “b”, the imperfection factor is $\alpha = 0.34$

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.457$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.34 \times (0.457 - 0.2) + 0.457^2 \right] = 0.648$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 + \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.648 + \sqrt{0.648^2 + 0.457^2}}, 1.0 \right) = 0.903$$

The confinement effect is also ignored since the eccentricity is larger than 0.1D.

○ M-N interaction curve

Point A ($0, N_{pl,Rd}$):

$$\begin{aligned} N_{pl,Rd} &= A_a f_{yd} + A_s f_{sd} + A_e f_{ed} + A_c f_{cd} \\ &= [(19458 + 13500) \times 355 + 3770 \times 400 + 165955 \times 48] \times 10^{-3} = 21187 \text{ kN} \end{aligned}$$

$$\text{Buckling resistance: } \chi N_{pl,Rd} = 0.903 \times 21187 = 19132 \text{ kN}$$

Point B ($M_{pl,Rd}, 0$):

$$\begin{aligned} h_n &= \frac{A_c f_{cd}}{2Df_{cd} + 4t_a(2f_{yd} - f_{cd}) + 4t_s(2f_{sd} - f_{cd}) + 2t_w(2f_{ed} - f_{cd})} \\ &= \frac{165955 \times 48}{2 \times 508 \times 48 + 4 \times 12.5 \times (2 \times 355 - 48) + 4 \times 2.94 \times (2 \times 400 - 48) + 2 \times 12.8 \times (2 \times 355 - 48)} \\ &= 73.7 \text{ mm} \end{aligned}$$

$h_n = 73.7 \text{ mm} < h/2 - t_f = 266.7/2 - 20.5 = 112.85 \text{ mm}$, thus, the neutral axial also lies in the web of the encased section.

$$W_{a,n} = 2t_a h_n^2 = 2 \times 12.5 \times 73.7^2 \times 10^{-3} = 135.8 \text{ cm}^3$$

$$W_{s,n} = 2t_s h_n^2 = 2 \times 2.94 \times 73.7^2 \times 10^{-3} = 31.9 \text{ cm}^3$$

$$W_{ey,n} = t_w h_n^2 = 12.8 \times 73.7^2 \times 10^{-3} = 69.5 \text{ cm}^3$$

$$W_{cy,n} = (D - 2t_a - 2t_s - t_w) h_n^2 = (508 - 2 \times 12.5 - 2 \times 2.94 - 12.8) \times 73.7^2 \times 10^{-3} = 2522 \text{ cm}^3$$

$$\begin{aligned}
M_{pl,Rd} &= (W_a - W_{a,n}) f_{yd} + (W_s - W_{s,n}) f_{sd} + (W_{ey} - W_{ey,n}) f_{ed} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\
&= [(3070 - 135.8) \times 355 + (489 - 31.9) \times 400 + (1469 - 65.9) \times 355 + 0.5 \times (16821 - 2522) \times 33.3] \times 10^{-3} \\
&= 2065 \text{ kN} \cdot \text{m}
\end{aligned}$$

Point C ($M_{pl,Rd}$, $N_{pm,Rd}$):

$$N_{pm,Rd} = A_c f_{cd} = 165955 \times 48 \times 10^{-3} = 7964 \text{ kN}$$

Point D ($M_{max,Rd}$, $N_{pm,Rd}/2$):

$$\begin{aligned}
M_{max,Rd} &= W_a f_{yd} + W_s f_{sd} + W_{ey} f_{ed} + 0.5 W_{cy} f_{cd} \\
&= [3070 \times 355 + 489 \times 400 + 1469 \times 355 + 0.5 \times 16821 \times 48] \times 10^{-3} \\
&= 2211 \text{ kN} \cdot \text{m}
\end{aligned}$$

- Steel contribution ratio

$$\begin{aligned}
\delta &= (A_a f_{yd} + A_e f_{ed}) / N_{pl,Rd} \\
&= (19458 + 13500) \times 355 \times 10^{-3} / 21187 = 0.552 < 0.9
\end{aligned}$$

2.4 CHS 508x12.5 and UC 254x254x107 - S500 steel sections with C50/60 concrete and G460 reinforcements

In this section, the mild steel S355 is replaced by the high tensile steel (HTS) S500, the concrete grade is not changed.

- Characteristic plastic resistance of cross-section

$$\begin{aligned}
N_{pl,Rk} &= A_a f_y + A_s f_{sk} + A_e f_{ek} + A_c f_{ck} \\
&= [(19458 + 13500) \times 500 + 3770 \times 460 + 165955 \times 50] \times 10^{-3} = 26530 \text{ kN}
\end{aligned}$$

- Relative slenderness ratio, buckling curves and buckling reduction factors

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{26530}{130793}} = 0.450 < 0.5$$

$$\bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{26530}{116984}} = 0.476 < 0.5$$

For buckling curves about both axis “b”, the imperfection factor is $\alpha = 0.34$

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.476$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.34 \times (0.476 - 0.2) + 0.476^2 \right] = 0.660$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 + \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.660 + \sqrt{0.660^2 + 0.476^2}}, 1.0 \right) = 0.895$$

The confinement effect is also ignored since the eccentricity is larger than 0.1D.

○ M-N interaction curve

Point A (0, $N_{pl,Rd}$):

$$\begin{aligned} N_{pl,Rd} &= A_a f_{yd} + A_s f_{sd} + A_e f_{ed} + A_c f_{cd} \\ &= [(19458 + 13500) \times 500 + 3770 \times 400 + 165955 \times 33.3] \times 10^{-3} = 23538 \text{ kN} \end{aligned}$$

Buckling resistance: $\chi N_{pl,Rd} = 0.895 \times 23538 = 21067 \text{ kN}$

Point B ($M_{pl,Rd}$, 0):

$$\begin{aligned} h_n &= \frac{A_c f_{cd}}{2Df_{cd} + 4t_a(2f_{yd} - f_{cd}) + 4t_s(2f_{sd} - f_{cd}) + 2t_w(2f_{ed} - f_{cd})} \\ &= \frac{165955 \times 33.3}{2 \times 508 \times 33.3 + 4 \times 12.5 \times (2 \times 500 - 33.3) + 4 \times 2.94 \times (2 \times 400 - 33.3) + 2 \times 12.8 \times (2 \times 500 - 33.3)} \\ &= 47.3 \text{ mm} \end{aligned}$$

The neutral axial also lies in the web of the encased section.

$$W_{a,n} = 2t_a h_n^2 = 2 \times 12.5 \times 47.3^2 \times 10^{-3} = 55.9 \text{ cm}^3$$

$$W_{s,n} = 2t_s h_n^2 = 2 \times 2.94 \times 47.3^2 \times 10^{-3} = 13.2 \text{ cm}^3$$

$$W_{ey,n} = t_w h_n^2 = 12.8 \times 47.3^2 \times 10^{-3} = 28.6 \text{ cm}^3$$

$$W_{cy,n} = (D - 2t_a - 2t_s - t_w) h_n^2 = (508 - 2 \times 12.5 - 2 \times 2.94 - 12.8) \times 47.3^2 \times 10^{-3} = 1039 \text{ cm}^3$$

$$\begin{aligned} M_{pl,Rd} &= (W_a - W_{a,n}) f_{yd} + (W_s - W_{s,n}) f_{sd} + (W_{ey} - W_{ey,n}) f_{ed} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\ &= [(3070 - 55.9) \times 500 + (489 - 13.2) \times 400 + (1469 - 28.6) \times 500 + 0.5 \times (16821 - 1039) \times 33.3] \times 10^{-3} \\ &= 2681 \text{ kN} \cdot \text{m} \end{aligned}$$

Point C ($M_{pl,Rd}$, $N_{pm,Rd}$):

$$N_{pm,Rd} = A_c f_{cd} = 165955 \times 33.3 \times 10^{-3} = 5530 \text{ kN}$$

Point D ($M_{max,Rd}$, $N_{pm,Rd}/2$):

$$\begin{aligned} M_{max,Rd} &= W_a f_{yd} + W_s f_{sd} + W_{ey} f_{ed} + 0.5 W_{cy} f_{cd} \\ &= [3070 \times 500 + 489 \times 400 + 1469 \times 500 + 0.5 \times 16821 \times 33.3] \times 10^{-3} \\ &= 2746 \text{ kN} \cdot \text{m} \end{aligned}$$

- Steel contribution ratio:

$$\begin{aligned} \delta &= (A_a f_{yd} + A_e f_{ed}) / N_{pl,Rd} \\ &= (19458 + 13500) \times 500 \times 10^{-3} / 23538 = 0.701 < 0.9 \end{aligned}$$

2.5 Comparison and summary

The design resistances are compared for the aforementioned three composite sections. The composite section with steel tube of S355, encased steel section of S355, concrete of C50/60, and reinforcing steel of G460 is referred to for the comparison.

It can be seen in Table 1, the axial buckling resistance ($\chi N_{pl,Rd}$) of the CFST column is improved by 11.6 % by use of high strength concrete C90/105 replacing normal strength concrete C50/60. However the increase of moment resistances ($M_{pl,Rd}$ and $M_{max,Rd}$) are smaller (less than 6%).

By use of steel S500 replacing S355, the axial buckling resistance is improved by 22.9%, and the increase of moment resistance is higher than 30%.

Table 1: Comparisons between circular CFST columns with various material strengths

Material grades (Steel+ Concrete+ Rebars)	Steel contribution ratios	Design resistances			
		$\chi N_{pl,Rd}$	$N_{pm,Rd}$	$M_{pl,Rd}$	$M_{max,Rd}$
S355+C50/60+G460	0.625	0	0	0	0
S355+C90/105+G460	0.552	11.6%	44.0%	2.9%	5.9%
S500+C50/60+G460	0.701	22.9%	0	33.6%	31.5%

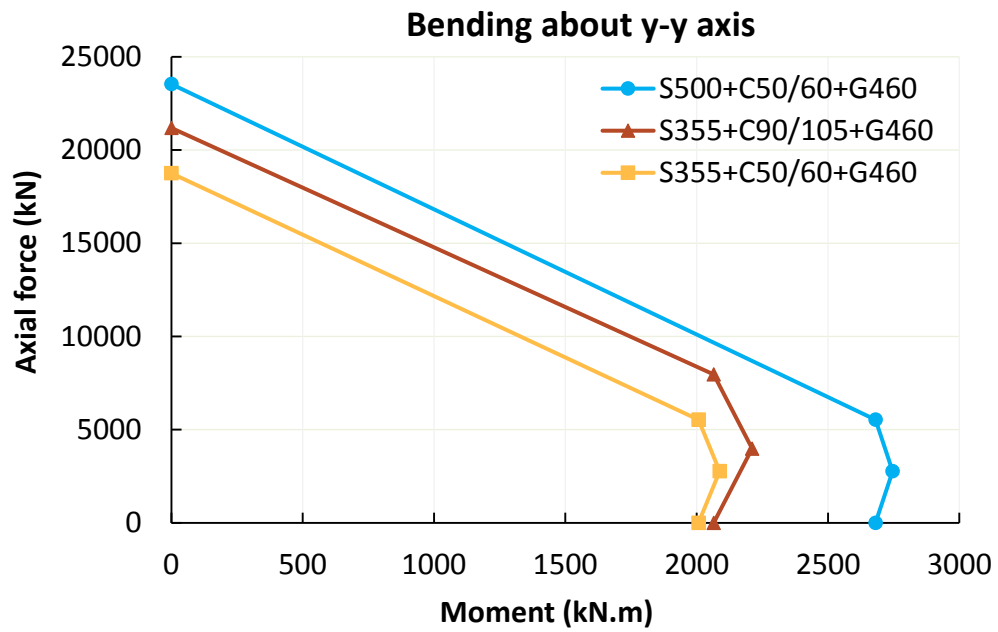


Figure 8: Design M-N interaction curves for CFST columns with various material grades

3 Example 3

3.1 General

In Example 3, the design resistance of a rectangular concrete filled steel tubular column are checked against combined axial compression and bi-axial bending moments. The dimensions of the rectangular CFST column are shown in Figure 9.

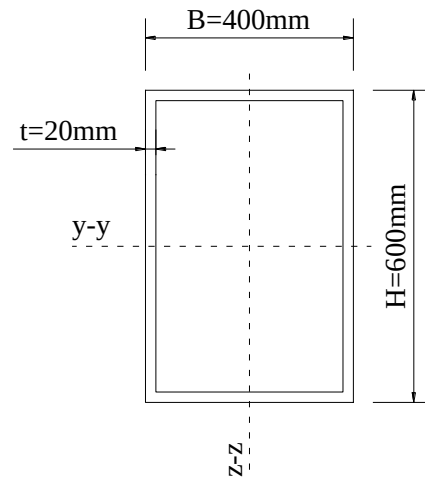
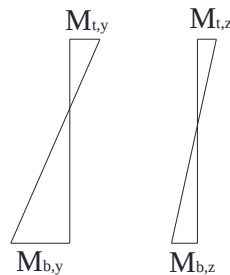


Figure 9: Cross-sectional dimensions of CFST column in Example 3

The column lengths and design loads are given as:

Column system length	$L=6000$ mm
Effective length	$L_{\text{eff}}=6000$ mm
Total design axial load	$N_{\text{Ed}}=12000$ kN
Design axial load that is permanent	$N_{\text{G,Ed}}=5000$ kN
Design moment at bottom around y-y axis	$M_{\text{b,y}}=900$ kN.m
Design moment at top around y-y axis	$M_{\text{t,y}}=-550$ kN.m



Design moment at bottom around y-y axis	$M_{\text{b,z}}=-600$ kN.m
Design moment at top around y-y axis	$M_{\text{t,z}}=350$ kN.m

To evaluate and compare their resistance, the following steel and concrete material grades are taken into account:

- a) RHS 400x600x20 - S355 steel with C50/60 concrete
- b) RHS 400x600x20 - S355 steel with C90/105 concrete
- c) RHS 400x600x20 - S500 steel with C50/60 concrete
- d) RHS 400x600x20 - S500 steel with C90/105 concrete

3.2 RHS 400x600x20 - S355 steel tube infilled with C50/60 concrete

○ Material

Concrete C50/60, $f_{ck}=50 \text{ N/mm}^2$

Steel tube Grade S355, $f_y=355 \text{ N/mm}^2$

○ Design strengths and modulus of material

$$f_{yd} = f_y / \gamma_a = 355 / 1.0 = 355 \text{ N/mm}^2$$

$$f_{cd} = f_{ck} / \gamma_c = 50 / 1.5 = 33.3 \text{ N/mm}^2$$

$$f_{cm} = f_{ck} + 8 = 50 + 8 = 58 \text{ N/mm}^2$$

$$E_a = 210 \text{ GPa}$$

$$E_{cm} = 22 (f_{cm} / 10)^{0.3} = 22 (58 / 10)^{0.3} = 37.3 \text{ GPa}$$

○ Cross sectional areas

$$A = BH = 400 \times 600 \times 10^{-2} = 2400 \text{ cm}^2$$

$$A_u = [BH - (B - 2t_a)(H - 2t_a)] = [400 \times 600 - (400 - 2 \times 20)(600 - 2 \times 20)] \times 10^{-2} = 384 \text{ cm}^2$$

$$A_c = A - A_u = 240000 - 38400 \times 10^{-2} = 2016 \text{ cm}^2$$

○ Second moment of areas

$$I_y = BH^3 / 12 = 400 \times 600^3 / 12 \times 10^{-4} = 720000 \text{ cm}^4$$

$$I_z = HB^3 / 12 = 600 \times 400^3 / 12 \times 10^{-4} = 320000 \text{ cm}^4$$

$$I_{ay} = [BH^3 - (B - 2t_a)(H - 2t_a)^3] / 12 = [400 \times 600^3 - (400 - 2 \times 20)(600 - 2 \times 20)^3] / 12 \times 10^{-4} \\ = 193152 \text{ cm}^4$$

$$I_{az} = \left[HB^3 - (H - 2t_a)(B - 2t_a)^3 \right] / 12 = \left[600 \times 400^3 - (600 - 2 \times 20)(400 - 2 \times 20)^3 \right] / 12 \times 10^{-4}$$

$$= 102272 \text{ cm}^4$$

$$I_{cy} = I_y - I_{ay} = 720000 - 193152 = 526848 \text{ cm}^4$$

$$I_{cz} = I_z - I_{az} = 320000 - 193152 = 217728 \text{ cm}^4$$

○ Plastic modulus

$$W_y = BH^2/4 = 400 \times 600^2/4 \times 10^{-3} = 36000 \text{ cm}^3$$

$$W_z = HB^2/4 = 600 \times 400^2/4 \times 10^{-3} = 24000 \text{ cm}^3$$

$$W_{ay} = \left[BH^2 - (B - 2t_a)(H - 2t_a)^2 \right] / 4 = \left[400 \times 600^2 - (400 - 2 \times 20)(600 - 2 \times 20)^2 \right] / 4 \times 10^{-3}$$

$$= 7776 \text{ cm}^3$$

$$W_{az} = \left[HB^2 - (H - 2t_a)(B - 2t_a)^2 \right] / 4 = \left[600 \times 400^2 - (600 - 2 \times 20)(400 - 2 \times 20)^2 \right] / 4 \times 10^{-3}$$

$$= 5856 \text{ cm}^3$$

$$W_{cy} = W_y - W_{ay} = 36000 - 7776 = 28224 \text{ cm}^3$$

$$W_{cz} = W_z - W_{az} = 24000 - 5856 = 18144 \text{ cm}^3$$

○ Check for local buckling

$$H/t_a = 600/20 = 30 < 52(235/f_y) = 52(235/355) = 42.3$$

Resistance against local buckling is adequate!

○ Long-term effect

Assuming age of concrete at loading in days: $t_0 = 30$

Age of concrete at moment considered in days: $t = \infty$

Relative humidity of ambient environment: RH=50%

Perimeter of concrete section: $u = 2(B - 2t_a) + 2(H - 2t_a)$

$$= 2(400 - 2 \times 20) + 2(600 - 2 \times 20) = 1840 \text{ mm}$$

Notional size of concrete section: $h_0 = 2A_c/u = 2 \times 201600/1840 = 219 \text{ mm}$

Coefficient: $\alpha_1 = (35/f_{cm})^{0.7} = (35/58)^{0.7} = 0.70$

Coefficient: $\alpha_2 = (35/f_{cm})^{0.2} = (35/58)^{0.2} = 0.90$

Coefficient: $\alpha_3 = (35/f_{cm})^{0.5} = (35/58)^{0.5} = 0.78$

Factor: $\varphi_{RH} = \left(1 + \frac{1 - RH/100}{0.1\sqrt[3]{h_0}}\alpha_1\right)\alpha_2 = \left(1 + \frac{1 - 50/100}{0.1\sqrt[3]{219}} \times 0.70\right) \times 0.90 = 1.43$

Factor: $\beta(f_{cm}) = 16.8/\sqrt{f_{cm}} = 16.8/\sqrt{58} = 2.21$

Factor: $\beta(t_0) = 1/(0.1 + t_0^{0.2}) = 1/(0.1 + 30^{0.2}) = 0.48$

Factor: $\varphi_0 = \varphi_{RH}\beta(f_{cm})\beta(t_0) = 1.43 \times 2.21 \times 0.48 = 1.52$

Factor: $\beta_H = 1.5 \left[1 + (0.012RH)^{18}\right]h_0 + 250\alpha_3$
 $= 1.5 \times \left[1 + (0.012 \times 50)^{18}\right] \times 219 + 250 \times 0.78 = 523$

Factor: $\beta_c(t, t_0) = \left(\frac{t - t_0}{\beta_H + t - t_0}\right)^{0.3} = \left(\frac{\infty - 14}{522 + \infty - 14}\right)^{0.3} = 1.0$

Creep coefficient: $\varphi_t = \varphi_0\beta_c(t, t_0) = 1.52 \times 1.0 = 1.52$

- Elastic modulus of concrete considering long-term effect

$$E_{c,eff} = E_{cm} \frac{1}{1 + (N_{G,Ed}/N_{Ed})\varphi_t} = \frac{37.3}{1 + (5000/12000) \times 1.52} = 22.8 \text{ GPa}$$

- Effective flexural stiffness of cross-section

$$(EI)_{eff,y} = E_a I_{ay} + 0.6 E_{c,eff} I_{cy}$$

$$= [210 \times 193152 + 0.6 \times 22.8 \times 526848] \times 10^4 = 4.78 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

$$(EI)_{eff,z} = E_a I_{az} + 0.6 E_{c,eff} I_{cz}$$

$$= [210 \times 102272 + 0.6 \times 22.8 \times 217728] \times 10^4 = 2.45 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

- Elastic critical Euler buckling resistance

$$N_{cr,y} = \frac{\pi^2 (EI)_{eff,y}}{L_{eff}^2} = \frac{\pi^2 \times 4.78 \times 10^{11}}{6000^2} = 130977 \text{ kN}$$

$$N_{cr,z} = \frac{\pi^2 (EI)_{eff,z}}{L_{eff}^2} = \frac{\pi^2 \times 2.45 \times 10^{11}}{6000^2} = 67053 \text{ kN}$$

- Characteristic plastic resistance of cross-section

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = [384 \times 355 + 2016 \times 50] \times 10^{-1} = 23712 \text{ kN}$$

- Relative slenderness ratio

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{23712}{130977}} = 0.425$$

$$\bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{23712}{67053}} = 0.595$$

- Buckling curves and buckling reduction factors

The buckling curves about both axis are “a”. Thus, the imperfection factor is $\alpha = 0.21$.

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = \max(0.425, 0.595) = 0.595$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.595 - 0.2) + 0.595^2 \right] = 0.718$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.718 + \sqrt{0.718^2 - 0.595^2}}, 1.0 \right) = 0.892$$

- Simplified Interaction Curves

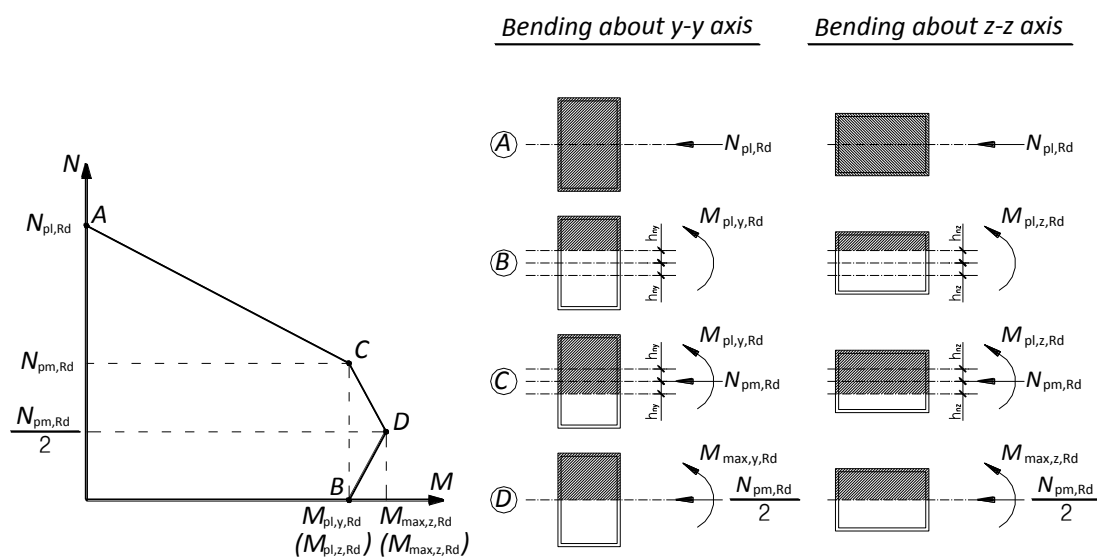


Figure 10: Simplified interaction curve for rectangular CFST columns

1) Point A ($0, N_{pl,Rd}$):

Confinement effect is not taken into account for rectangular CFST column, thus

$$N_{pl,Rd} = A_a f_{yd} + A_c f_{cd} = [384 \times 355 + 2016 \times 33.3] \times 10^{-1} = 20352 \text{ kN}$$

$$\text{Buckling resistance: } \chi N_{pl,Rd} = 0.892 \times 20352 = 18154 \text{ kN}$$

2) Point B ($M_{pl,y,Rd}, 0$) & ($M_{pl,z,Rd}, 0$):

The position of neutral axis are determined from

$$h_{ny} = \frac{A_c f_{cd}}{2Bf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 33.3}{2 \times 400 \times 33.3 + 4 \times 20 \times (2 \times 355 - 33.3)} = 83.2 \text{ mm}$$

$$h_{nz} = \frac{A_c f_{cd}}{2Hf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 33.3}{2 \times 600 \times 33.3 + 4 \times 20 \times (2 \times 355 - 33.3)} = 71.4 \text{ mm}$$

The plastic modulus of steel tube and concrete in the height of $2h_n$, bending about centreline of the cross-section are calculated as:

$$W_{ay,n} = 2t_a h_{ny}^2 = 2 \times 20 \times 83.2^2 \times 10^{-3} = 276.9 \text{ cm}^3$$

$$W_{az,n} = 2t_a h_{nz}^2 = 2 \times 20 \times 71.4^2 \times 10^{-3} = 204 \text{ cm}^3$$

$$W_{cy,n} = (B - 2t_a) h_{ny}^2 = (400 - 2 \times 20) \times 83.2^2 \times 10^{-3} = 2492 \text{ cm}^3$$

$$W_{cz,n} = (H - 2t_a) h_{nz}^2 = (600 - 2 \times 20) \times 71.4^2 \times 10^{-3} = 2855 \text{ cm}^3$$

Taking moment about the centreline of the cross-section, the plastic bending resistance is determined from:

$$\begin{aligned} M_{pl,y,Rd} &= (W_{ay} - W_{ay,n}) f_{yd} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\ &= [(7776 - 276.9) \times 355 + 0.5 \times (28224 - 2492) \times 33.3] \times 10^{-3} \\ &= 3091 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{pl,z,Rd} &= (W_{az} - W_{az,n}) f_{yd} + 0.5(W_{cz} - W_{cz,n}) f_{cd} \\ &= [(5856 - 204) \times 355 + 0.5 \times (18144 - 2855) \times 33.3] \times 10^{-3} \\ &= 2261 \text{ kN} \cdot \text{m} \end{aligned}$$

3) Point C ($M_{pl,y,Rd}, N_{pm,Rd}$) & ($M_{pl,z,Rd}, N_{pm,Rd}$):

$$N_{pm,Rd} = A_c f_{cd} = 201600 \times 33.3 \times 10^{-3} = 6720 \text{ kN}$$

4) Point D ($M_{\max,y,Rd}$, $N_{pm,Rd}/2$) & ($M_{\max,z,Rd}$, $N_{pm,Rd}/2$):

$$\begin{aligned} M_{\max,y,Rd} &= W_{ay} f_{yd} + 0.5 W_{cy} f_{cd} \\ &= [7776 \times 355 + 0.5 \times 28224 \times 33.3] \times 10^{-3} \\ &= 3231 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{\max,z,Rd} &= W_{az} f_{yd} + 0.5 W_{cz} f_{cd} \\ &= [5856 \times 355 + 0.5 \times 18144 \times 33.3] \times 10^{-3} \\ &= 2381 \text{ kN} \cdot \text{m} \end{aligned}$$

- Steel contribution ratio

$$\begin{aligned} \delta &= A_a f_{yd} / N_{pl,Rd} = 384 \times 355 \times 10^{-1} / 20352 \\ &= 0.67 < 0.9 \end{aligned}$$

- Check for resistance of column in axial compression

$$\frac{N_{Ed}}{\chi N_{pl,Rd}} = \frac{12000}{0.892 \times 20352} = 0.661 < 1.0$$

Thus, the buckling resistance under axial compression is adequate!

- Check for resistance of column in combined compression and biaxial bending moments

The design value of effective flexural stiffness with long-term effect is calculated from:

$$\begin{aligned} (EI)_{eff,II,y} &= K_0 (E_a I_{ay} + K_{e,II} E_{c,m} I_{cy}) = 0.9 \times [210 \times 193152 + 0.5 \times 22.8 \times 526848] \times 10^4 \\ &= 4.19 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

$$\begin{aligned} (EI)_{eff,II,z} &= K_0 (E_a I_{az} + K_{e,II} E_{c,m} I_{cz}) = 0.9 \times [210 \times 102272 + 0.5 \times 22.8 \times 217728] \times 10^4 \\ &= 2.16 \times 10^{11} \text{ kN} \cdot \text{mm}^2 \end{aligned}$$

Thus, the critical normal forces with effective length taken as the system length of column are determined from:

$$N_{cr,eff,y} = \frac{\pi^2 (EI)_{eff,II,y}}{L^2} = \frac{\pi^2 \times 4.19 \times 10^{11}}{6000^2} = 114913 \text{ kN}$$

$$N_{cr,eff,z} = \frac{\pi^2 (EI)_{eff,\Pi,z}}{L^2} = \frac{\pi^2 \times 2.16 \times 10^{11}}{6000^2} = 59122 \text{ kN}$$

The second-order effect should be considered for both moments from first-order analysis and moment from imperfection, as shown in Figure 6. According to the buckling curve “a” and refer to Table 3.3 of BC4, the initial imperfections about y-y axis and z-z axis are:

$$e_{0,y} = L/300 = 6000/300 = 20 \text{ mm}$$

$$e_{0,z} = L/300 = 6000/300 = 20 \text{ mm}$$

Accordingly, the bending moments by the initial imperfections are determined as:

$$M_{0,y} = N_{Ed} e_{0,y} = 12000 \times 20/1000 = 240 \text{ kN} \cdot \text{m}$$

$$M_{0,z} = N_{Ed} e_{0,z} = 12000 \times 20/1000 = 240 \text{ kN} \cdot \text{m}$$

According to the moment diagram by the initial imperfection, the factor β_0 for determination of moment to second-order effect is equal to 1.0. Thus, the amplification factors for the moments by the imperfection are calculated from:

$$k_{0,y} = \frac{\beta_0}{1 - N_{Ed}/N_{cr,eff,y}} = \frac{1.0}{1 - 12000/114913} = 1.117$$

$$k_{0,z} = \frac{\beta_0}{1 - N_{Ed}/N_{cr,eff,z}} = \frac{1.0}{1 - 12000/59122} = 1.255$$

According to the first-order design moment diagram, the ratio of end moments is calculated as:

$$r_y = M_{t,y}/M_{b,y} = -550/900 = -0.611$$

$$r_z = M_{t,z}/M_{b,z} = 350/(-600) = -0.583$$

Thus, the factors for determination of moment to second-order effect are determined:

$$\beta_{1,y} = \max(0.66 + 0.44r_y, 0.44) = \max(0.66 + 0.44 \times (-0.611), 0.44) = 0.44$$

$$\beta_{1,z} = \max(0.66 + 0.44r_z, 0.44) = \max(0.66 + 0.44 \times (-0.583), 0.44) = 0.44$$

Thus, the amplification factors for the moment by the imperfection are calculated from:

$$k_{1,y} = \frac{\beta_{1,y}}{1 - N_{Ed}/N_{cr,eff,y}} = \frac{0.44}{1 - 12000/114913} = 0.491$$

$$k_{1,z} = \frac{\beta_{1,z}}{1 - N_{Ed}/N_{cr,eff,z}} = \frac{0.44}{1 - 12000/59122} = 0.552$$

Thus, the design moments, considering second-order effect, are calculated as:

$$\begin{aligned} M_{y,Ed} &= \text{Max} \left[k_{0,y} M_{0,y} + k_{1,y} \text{Max}(|M_{t,y}|, |M_{b,y}|), \text{Max}(|M_{t,y}|, |M_{b,y}|) \right] \\ &= \text{Max} [1.117 \times 240 + 0.491 \times \text{Max}(|-550|, |900|), \text{Max}(|-550|, |900|)] = 900 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{z,Ed} &= \text{Max} \left[k_{0,z} M_{0,z} + k_{1,z} \text{Max}(|M_{t,z}|, |M_{b,z}|), \text{Max}(|M_{t,z}|, |M_{b,z}|) \right] \\ &= \text{Max} [1.255 \times 240 + 0.552 \times \text{Max}(|350|, |-600|), \text{Max}(|350|, |-600|)] = 632 \text{ kN} \cdot \text{m} \end{aligned}$$

For $N_{Ed} = 12000 \text{ kN} > N_{pm,Rd} = 6720 \text{ kN}$, the values for determining the plastic bending resistances $M_{pl,N,y,Rd}$ and $M_{pl,N,z,Rd}$ taking into account the normal force N_{Ed} are calculated from:

$$\mu_{dy} = \mu_{dz} = \frac{N_{pl,Rd} - N_{Ed}}{N_{pl,Rd} - N_{pm,Rd}} = \frac{20352 - 12000}{20352 - 6720} = 0.613$$

$$\frac{M_{y,Ed}}{M_{pl,N,y,Rd}} = \frac{M_{y,Ed}}{\mu_{dy} M_{pl,y,Rd}} = \frac{900}{0.613 \times 3091} = 0.475 < \alpha_{M,y} = 0.9$$

$$\frac{M_{z,Ed}}{M_{pl,N,z,Rd}} = \frac{M_{z,Ed}}{\mu_{dz} M_{pl,z,Rd}} = \frac{632}{0.613 \times 2261} = 0.456 < \alpha_{M,z} = 0.9$$

$$\frac{M_{y,Ed}}{\mu_{dy} M_{pl,y,Rd}} + \frac{M_{z,Ed}}{\mu_{dz} M_{pl,z,Rd}} = \frac{900}{0.613 \times 3091} + \frac{632}{0.613 \times 2261} = 0.932 < 1.0$$

Thus, the resistance for combined axial compression and biaxial bending is adequate. The external design force and bending moment, and M-N interaction curves are plotted in Figure 11, Figure 12 and Figure 13.

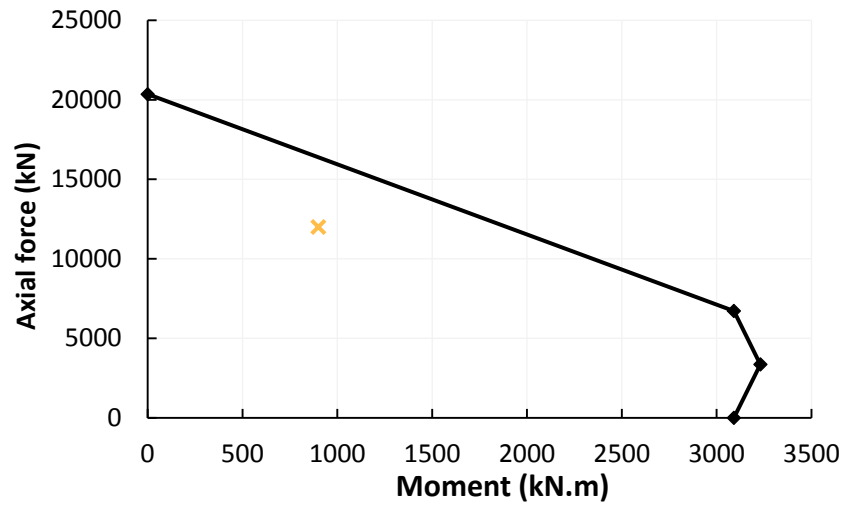


Figure 11: Design M-N curve for bending about y-y axis

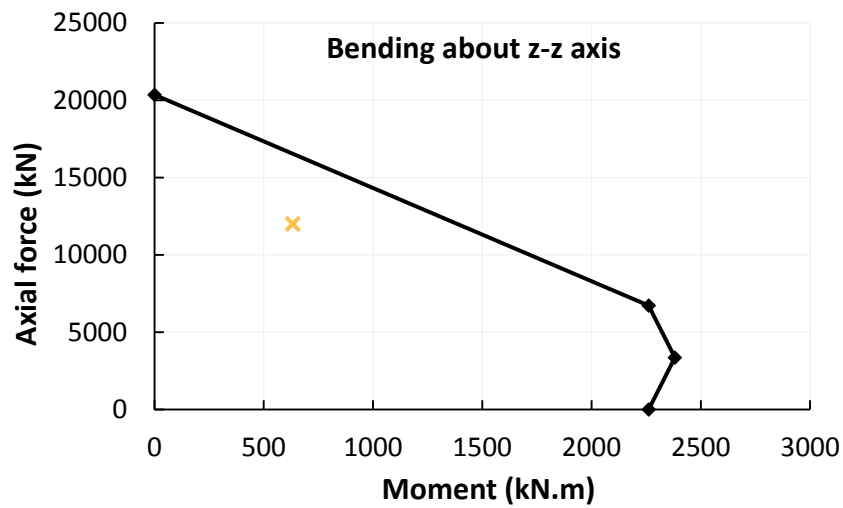


Figure 12: Design M-N curve for bending about z-z axis

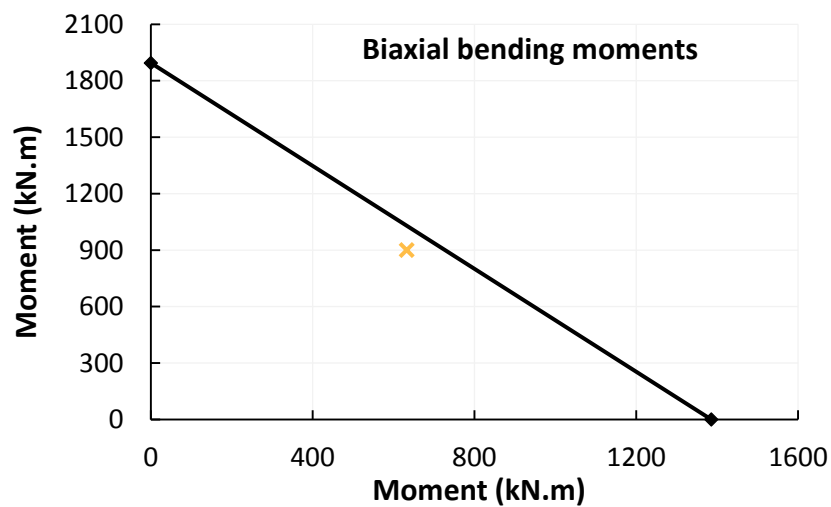


Figure 13: Check for bi-axial bending

3.3 RHS 400x600x20 - S355 steel tube infilled with C90/105 concrete

In this section, the high strength concrete C50/60 is replaced by higher strength concrete C90/105. The steel grade is not changed.

o Design strength

Effective compressive strength and modulus of elasticity are taken from to Table 2.2, Eq.(2.2) and Eq.(2.3) of BC4.

$$f_{ck} = 72 \text{ N/mm}^2; E_{cm} = 41.1 \text{ GPa}$$

$$f_{cd} = f_{ck} / \gamma_c = 72 / 1.5 = 48 \text{ N/mm}^2; f_{cm} = f_{ck} + 8 = 72 + 8 = 80 \text{ N/mm}^2$$

o Elastic modulus of concrete considering long-term effect

Creep coefficient could be similarly determined as $\varphi_t = 1.12$

$$E_{c,eff} = \frac{E_{cm}}{1 + (N_{G,Ed} / N_{Ed}) \varphi_t} = \frac{41.1}{1 + (5000 / 12000) \times 1.12} = 28 \text{ GPa}$$

o Effective flexural stiffness of cross-section

$$(EI)_{eff,y} = E_a I_{ay} + 0.6 E_{c,eff} I_{cy} = [210 \times 193152 + 0.6 \times 28 \times 526848] \times 10^4 = 4.94 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

$$(EI)_{eff,z} = E_a I_{az} + 0.6 E_{c,eff} I_{cz} = [210 \times 102272 + 0.6 \times 28 \times 217728] \times 10^4 = 2.51 \times 10^{11} \text{ kN} \cdot \text{mm}^2$$

o Characteristic plastic resistance of cross-section

$$N_{cr,y} = \frac{\pi^2 (EI)_{eff,y}}{L_{eff}^2} = \frac{\pi^2 \times 4.94 \times 10^{11}}{6000^2} = 135431 \text{ kN}$$

$$N_{cr,z} = \frac{\pi^2 (EI)_{eff,z}}{L_{eff}^2} = \frac{\pi^2 \times 2.51 \times 10^{11}}{6000^2} = 68893 \text{ kN}$$

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = [384 \times 355 + 2016 \times 90] \times 10^{-1} = 28147 \text{ kN}$$

o Relative slenderness ratio, buckling curves and buckling reduction factors

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{28147}{135431}} = 0.456; \bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{28147}{68893}} = 0.639$$

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.639$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.639 - 0.2) + 0.639^2 \right] = 0.75$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.75 + \sqrt{0.75^2 - 0.639^2}}, 1.0 \right) = 0.875$$

$$N_{pl,Rd} = A_a f_{yd} + A_c f_{cd} = [384 \times 355 + 2016 \times 41.1] \times 10^{-1} = 23309 \text{ kN}$$

$$\text{Buckling resistance: } \chi N_{pl,Rd} = 0.875 \times 23309 = 20395 \text{ kN}$$

o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = 384 \times 355 \times 10^{-1} / 23309 = 0.585 < 0.9$$

o M-N interaction curve

$$h_{ny} = \frac{A_c f_{cd}}{2Bf_{cd} + 4t_a (2f_{yd} - f_{cd})} = \frac{201600 \times 41.1}{2 \times 400 \times 41.1 + 4 \times 20 \times (2 \times 355 - 41.1)} = 105.9 \text{ mm}$$

$$h_{nz} = \frac{A_c f_{cd}}{2Hf_{cd} + 4t_a (2f_{yd} - f_{cd})} = \frac{201600 \times 41.1}{2 \times 600 \times 41.1 + 4 \times 20 \times (2 \times 355 - 41.1)} = 87.5 \text{ mm}$$

$$W_{ay,n} = 2t_a h_{ny}^2 = 2 \times 20 \times 105.9^2 \times 10^{-3} = 448.6 \text{ cm}^3$$

$$W_{az,n} = 2t_a h_{nz}^2 = 2 \times 20 \times 87.5^2 \times 10^{-3} = 306.3 \text{ cm}^3$$

$$W_{cy,n} = (B - 2t_a) h_{ny}^2 = (400 - 2 \times 20) \times 105.9^2 \times 10^{-3} = 4037.3 \text{ cm}^3$$

$$W_{cz,n} = (H - 2t_a) h_{nz}^2 = (600 - 2 \times 20) \times 87.5^2 \times 10^{-3} = 4287.5 \text{ cm}^3$$

$$\begin{aligned} M_{pl,y,Rd} &= (W_{ay} - W_{ay,n}) f_{yd} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\ &= [(7776 - 448.6) \times 355 + 0.5 \times (28224 - 4037.3) \times 41.1] \times 10^{-3} = 3182 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{pl,z,Rd} &= (W_{az} - W_{az,n}) f_{yd} + 0.5(W_{cz} - W_{cz,n}) f_{cd} \\ &= [(5856 - 306.3) \times 355 + 0.5 \times (18144 - 4287.5) \times 41.1] \times 10^{-3} = 2303 \text{ kN} \cdot \text{m} \end{aligned}$$

$$N_{pm,Rd} = A_c f_{cd} = 201600 \times 41.1 \times 10^{-3} = 9677 \text{ kN}$$

$$\begin{aligned} M_{\max,y,Rd} &= W_{ay} f_{yd} + 0.5W_{cy} f_{cd} \\ &= [7776 \times 355 + 0.5 \times 28224 \times 41.1] \times 10^{-3} = 3438 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned}
 M_{\max,z,Rd} &= W_{az} f_{yd} + 0.5 W_{cz} f_{cd} \\
 &= [5856 \times 355 + 0.5 \times 18144 \times 41.1] \times 10^{-3} = 2514 \text{ kN} \cdot \text{m}
 \end{aligned}$$

3.4 RHS 400x600x20 - S500 steel tube infilled with C50/60 concrete

In this section, the mild steel S355 is replaced by the high tensile steel (HTS) S500, the concrete grade is not changed.

○ Plastic resistance of cross-section

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = [384 \times 500 + 2016 \times 50] \times 10^{-1} = 29280 \text{ kN}$$

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{29280}{130977}} = 0.473; \bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{29280}{67053}} = 0.661$$

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.661$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.661 - 0.2) + 0.661^2 \right] = 0.767$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.767 + \sqrt{0.767^2 - 0.661^2}}, 1.0 \right) = 0.865$$

$$N_{pl,Rd} = A_a f_{yd} + A_c f_{cd} = [384 \times 500 + 2016 \times 33.3] \times 10^{-1} = 25920 \text{ kN}$$

$$\text{Buckling resistance: } \chi N_{pl,Rd} = 0.865 \times 25920 = 22421 \text{ kN}$$

○ Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = 384 \times 500 \times 10^{-1} / 22421 = 0.741 < 0.9$$

○ M-N interaction curve

$$h_{ny} = \frac{A_c f_{cd}}{2Bf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 33.3}{2 \times 400 \times 33.3 + 4 \times 20 \times (2 \times 500 - 33.3)} = 64.6 \text{ mm}$$

$$h_{nz} = \frac{A_c f_{cd}}{2Hf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 33.3}{2 \times 600 \times 33.3 + 4 \times 20 \times (2 \times 500 - 33.3)} = 57.3 \text{ mm}$$

$$W_{ay,n} = 2t_a h_{ny}^2 = 2 \times 20 \times 64.6^2 \times 10^{-3} = 170 \text{ cm}^3$$

$$W_{az,n} = 2t_a h_{nz}^2 = 2 \times 20 \times 57.3^2 \times 10^{-3} = 131.3 \text{ cm}^3$$

$$W_{cy,n} = (B - 2t_a) h_{ny}^2 = (400 - 2 \times 20) \times 64.6^2 \times 10^{-3} = 1502.3 \text{ cm}^3$$

$$W_{cz,n} = (H - 2t_a) h_{nz}^2 = (600 - 2 \times 20) \times 57.3^2 \times 10^{-3} = 1838.6 \text{ cm}^3$$

$$\begin{aligned} M_{pl,y,Rd} &= (W_{ay} - W_{ay,n}) f_{yd} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\ &= [(7776 - 170) \times 500 + 0.5 \times (28224 - 1502.3) \times 33.3] \times 10^{-3} = 4250 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{pl,z,Rd} &= (W_{az} - W_{az,n}) f_{yd} + 0.5(W_{cz} - W_{cz,n}) f_{cd} \\ &= [(5856 - 131.3) \times 500 + 0.5 \times (18144 - 1838.6) \times 33.3] \times 10^{-3} = 3134 \text{ kN} \cdot \text{m} \end{aligned}$$

$$N_{pm,Rd} = A_c f_{cd} = 201600 \times 33.3 \times 10^{-3} = 6720 \text{ kN}$$

$$\begin{aligned} M_{\max,y,Rd} &= W_{ay} f_{yd} + 0.5 W_{cy} f_{cd} \\ &= [7776 \times 500 + 0.5 \times 28224 \times 33.3] \times 10^{-3} = 4358 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{\max,z,Rd} &= W_{az} f_{yd} + 0.5 W_{cz} f_{cd} \\ &= [5856 \times 500 + 0.5 \times 18144 \times 33.3] \times 10^{-3} = 3230 \text{ kN} \cdot \text{m} \end{aligned}$$

3.5 RHS 400x600x20 - S500 steel tube infilled with C90/105 concrete

In this section, the mild steel S355 is replaced by the high tensile steel (HTS) S500, and the normal strength concrete C50/60 is replaced by high strength concrete C90/105.

○ Plastic resistance of cross-section

$$N_{pl,Rk} = A_a f_y + A_c f_{ck} = [384 \times 500 + 2016 \times 90] \times 10^{-1} = 33715 \text{ kN}$$

$$\bar{\lambda}_y = \sqrt{\frac{N_{pl,Rk}}{N_{cr,y}}} = \sqrt{\frac{33715}{135431}} = 0.499; \quad \bar{\lambda}_z = \sqrt{\frac{N_{pl,Rk}}{N_{cr,z}}} = \sqrt{\frac{33715}{68893}} = 0.7$$

$$\bar{\lambda} = \max(\bar{\lambda}_y, \bar{\lambda}_z) = 0.7$$

$$\Phi = 0.5 \left[1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2 \right] = 0.5 \left[1 + 0.21 \times (0.7 - 0.2) + 0.7^2 \right] = 0.797$$

$$\chi = \min \left(\frac{1}{\Phi + \sqrt{\Phi^2 - \bar{\lambda}^2}}, 1.0 \right) = \min \left(\frac{1}{0.797 + \sqrt{0.797^2 - 0.7^2}}, 1.0 \right) = 0.848$$

$$N_{pl,Rd} = A_a f_{yd} + A_c f_{cd} = [384 \times 500 + 2016 \times 41.1] \times 10^{-1} = 28877 \text{ kN}$$

Buckling resistance: $\chi N_{pl,Rd} = 0.848 \times 28877 = 24488 \text{ kN}$

o Steel contribution ratio

$$\delta = A_a f_{yd} / N_{pl,Rd} = 384 \times 500 \times 10^{-1} / 24488 = 0.665 < 0.9$$

o M-N interaction curve

$$h_{ny} = \frac{A_c f_{cd}}{2Bf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 41.1}{2 \times 400 \times 41.1 + 4 \times 20 \times (2 \times 500 - 41.1)} = 84.5 \text{ mm}$$

$$h_{nz} = \frac{A_c f_{cd}}{2Hf_{cd} + 4t_a(2f_{yd} - f_{cd})} = \frac{201600 \times 41.1}{2 \times 600 \times 41.1 + 4 \times 20 \times (2 \times 500 - 41.1)} = 72.3 \text{ mm}$$

$$W_{ay,n} = 2t_a h_{ny}^2 = 2 \times 20 \times 84.5^2 \times 10^{-3} = 285.6 \text{ cm}^3$$

$$W_{az,n} = 2t_a h_{nz}^2 = 2 \times 20 \times 72.3^2 \times 10^{-3} = 209.1 \text{ cm}^3$$

$$W_{cy,n} = (B - 2t_a) h_{ny}^2 = (400 - 2 \times 20) \times 84.5^2 \times 10^{-3} = 2570.5 \text{ cm}^3$$

$$W_{cz,n} = (H - 2t_a) h_{nz}^2 = (600 - 2 \times 20) \times 72.3^2 \times 10^{-3} = 2927.3 \text{ cm}^3$$

$$\begin{aligned} M_{pl,y,Rd} &= (W_{ay} - W_{ay,n}) f_{yd} + 0.5(W_{cy} - W_{cy,n}) f_{cd} \\ &= [(7776 - 285.6) \times 500 + 0.5 \times (28224 - 2570.5) \times 41.1] \times 10^{-3} = 4361 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{pl,z,Rd} &= (W_{az} - W_{az,n}) f_{yd} + 0.5(W_{cz} - W_{cz,n}) f_{cd} \\ &= [(5856 - 209.1) \times 500 + 0.5 \times (18144 - 2927.3) \times 41.1] \times 10^{-3} = 3188 \text{ kN} \cdot \text{m} \end{aligned}$$

$$N_{pm,Rd} = A_c f_{cd} = 201600 \times 41.1 \times 10^{-3} = 9677 \text{ kN}$$

$$\begin{aligned} M_{\max,y,Rd} &= W_{ay} f_{yd} + 0.5W_{cy} f_{cd} \\ &= [7776 \times 500 + 0.5 \times 28224 \times 41.1] \times 10^{-3} = 4565 \text{ kN} \cdot \text{m} \end{aligned}$$

$$\begin{aligned} M_{\max,z,Rd} &= W_{az} f_{yd} + 0.5W_{cz} f_{cd} \\ &= [5856 \times 500 + 0.5 \times 18144 \times 41.1] \times 10^{-3} = 3363 \text{ kN} \cdot \text{m} \end{aligned}$$

3.6 Comparison and summary

The design resistances are compared for the aforementioned four rectangular composite sections as shown in Table 2, Figure 14 and Figure 15. The composite section with steel tube of S355 and concrete of C50/60 is referred to for comparison.

By using high strength concrete C90/105 replacing normal strength concrete C50/60, the axial buckling resistance ($\chi N_{pl,Rd}$) of the CFST column is improved by 12.3%, and the increase of moment resistances ($M_{pl,y,Rd}$, $M_{pl,z,Rd}$, $M_{max,y,Rd}$, $M_{max,z,Rd}$) are smaller (less than 7%).

Table 2: Comparison between rectangular CFST columns with various material strengths

Sections	Steel contribution ratios	Design resistances				
		$\chi N_{pl,Rd}$	$M_{pl,y,Rd}$	$M_{pl,z,Rd}$	$M_{max,y,Rd}$	$M_{max,z,Rd}$
S355+C50/60	0.670	0	0	0	0	0
S355+C90/105	0.585	12.3%	2.9%	1.8%	6.4%	5.6%
S500+C50/60	0.741	23.5%	37.5%	38.6%	34.9%	35.6%
S500+C90/105	0.665	34.9%	41.1%	41.0%	41.3%	41.2%

By using high strength steel S500 to replace S355 steel, the axial buckling resistance is improved by 23.5%, and the increase of moment resistances are larger (higher than 34.9%). By using high strength concrete C90/105 to replace normal strength concrete C50/60 and use of S500 steel to replace S355 steel, the axial buckling resistance is further improved to 34.9%, and the increase of moment resistances are more than 40%.

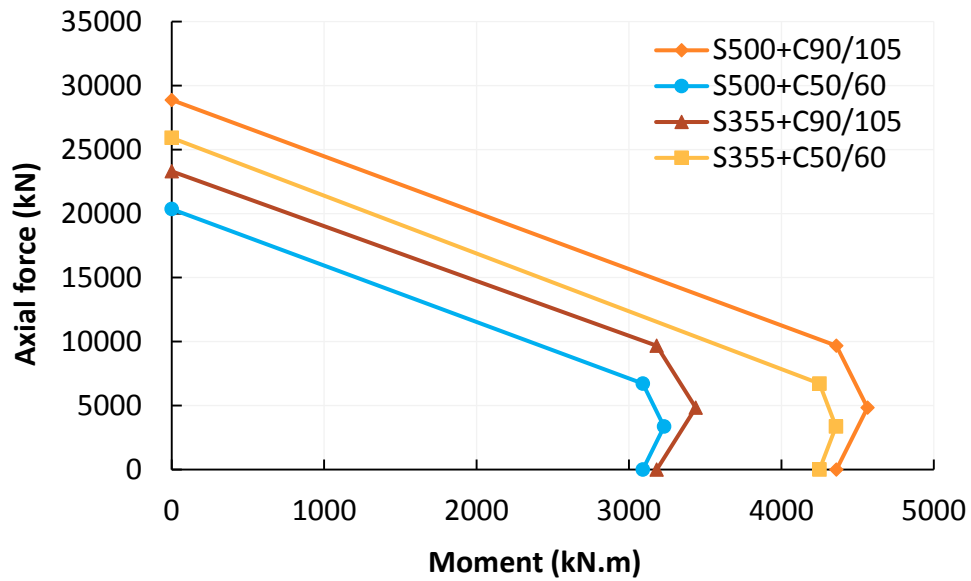


Figure 14: Design M-N interaction curves about y-y axis

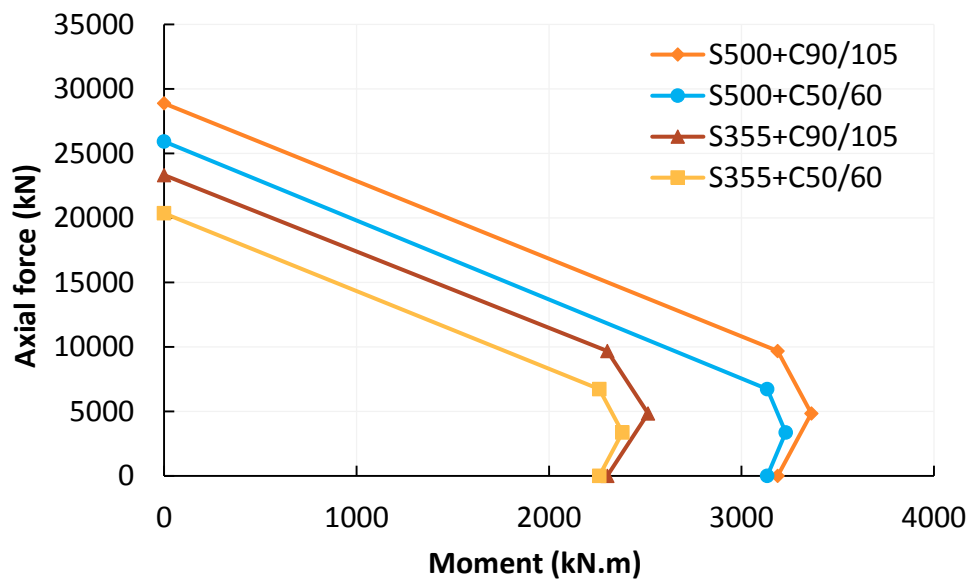


Figure 15: Design M-N interaction curves about z-z axis